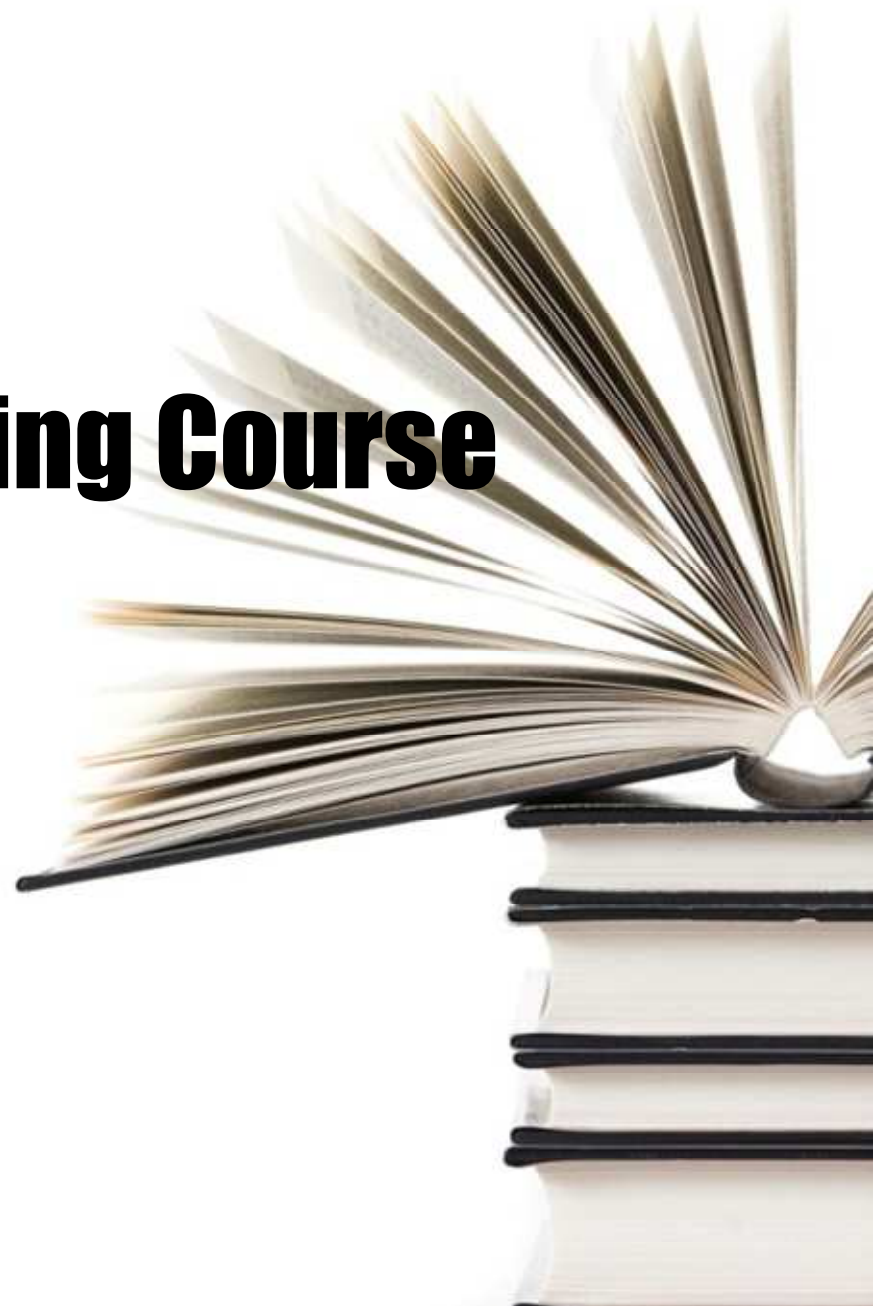


OpenMP Training Course

Part 2 Advanced



<http://www.ksc.re.kr>
<http://edu.ksc.re.kr>





Resources



- <http://edu.ksc.re.kr>
- <http://www.openmp.org>
- <http://www.compunity.org>
- <https://computing.llnl.gov/tutorials/openMP/>
- <http://www.citutor.org>
- <http://docs.oracle.com/cd/E19422-01/819-3694/>





Agenda (Advanced Course)



- 09:30 – 10:00 Brief Review & Introduction to Education System
- 10:00 – 12:00 Work Sharing & Synchronization
- 12:00 – 13:30 Lunch
- 13:30 – 14:50 Schedule & Task
- 14:50 – 15:00 Break
- 15:00 – 16:30 OpenMP Performance & Hands-on
- 16:30 – 17:00 Summary



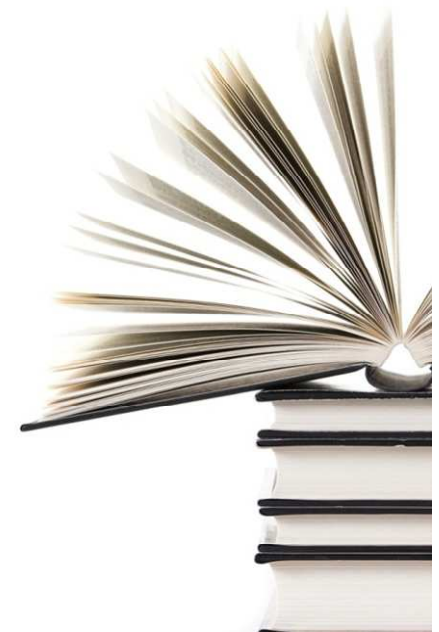
Agenda (Advanced Course)



- Brief Review
 - OpenMP Basics (Create Threads, Data Scope, Loop, Synchronization, Reduction)
- Introduction to Education System
 - Check Environment
- Create Threads [2.4, 3.2] (Nested Parallelism)
- Work Sharing
 - sections [2.5.2, 2.6.2], single [2.5.3], master [2.8.1]
- Synchronization
 - nowait, ordered [2.8.7], lock [3.3]
- Task
 - task [2.7.1], taskwait [2.8.4]
- Schedule [3.2]
- OpenMP Performance
 - Nested Parallel (Collapse)
 - Flush [2.8.6]
 - False Sharing
 - Data DepENDency
- Hands-on
 - Triangular Matrix Multiplication
 - LU Decomposition (Optional)
 - Fibonacci (Optional)
- Summary

Introduction to Education System

- 1. Education System**
- 2. Check Environment**



PuTTY 설정

문류(G)

- 세션
 - 로그인
 - 터미널
 - 키보드
 - 벨
 - 기능
 - 창
 - 모양
 - 특성
 - 변환
 - 선택
 - 색깔
 - 접속
 - 데이터
 - 프락시
 - 텔넷
 - rlogin
 - SSH
 - 시리얼

PuTTY 세션 기본 옵션

접속 대상 정보

Host Name (or IP address) Port

접속 형식:

☐ 생짜 (R) ☐ Telnet ☐ Rlogin ☒ SSH ☐ 시리얼

저장된 세션의 불러오기, 저장, 지움

저장된 세션 (E)

교육용슈퍼컴

기본 설정

교육용슈퍼컴

불러옴(L) 저장(V) 지움(D)

종료시에 창을 닫음 (W):

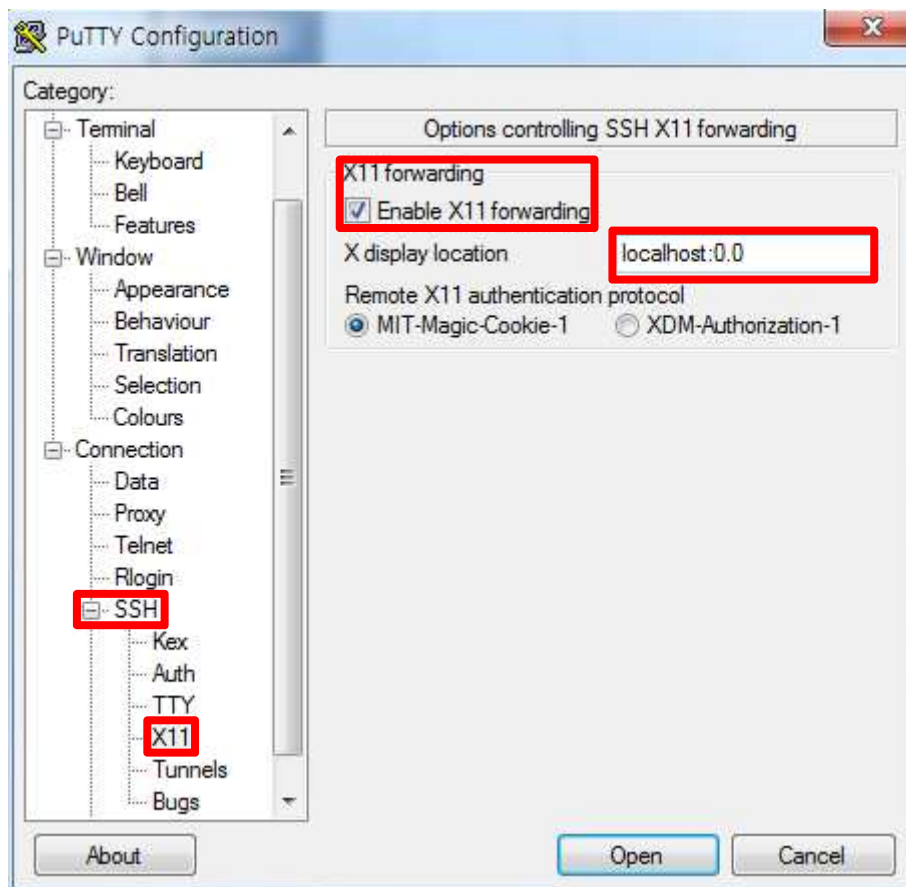
☐ 항상 ☐ 안 닫음 ☒ 접속이 끊겼을 때만

도움 도움 (H) 열기 (O) 취소 (C)

Putty 설정



- ssh => X11 [Enable X11 forwarding] 체크
- X display location : localhost : 0.0
- save



윈도우에서
Xming 실행

➤ PuTTY Security Alert [예(y)] 선택





Putty 설정



- login as :
- edun##@xxx.xxx.xxx.xxx's password :

```
edun20@master01:~  
login as: edun20  
edun20@ password:  
Last login: Wed Sep 21 11:08:31 2011 from 150.183.108.120  
998% [edun20@master01 ~]#
```

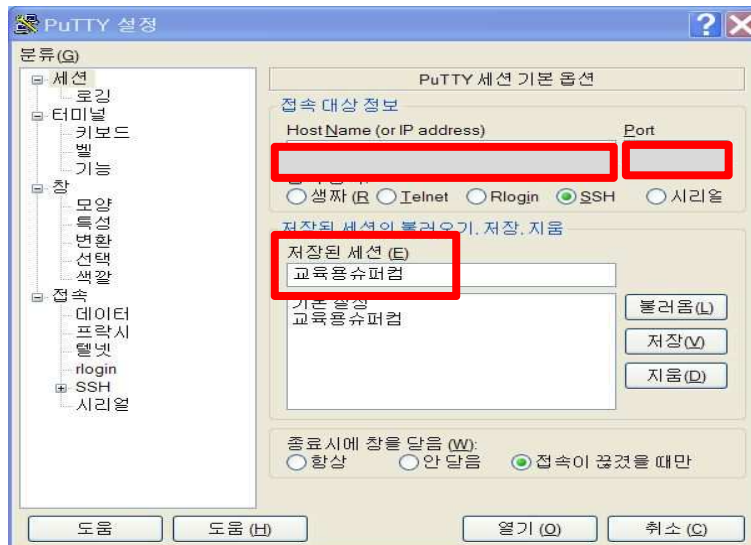
- Freeware
- 다운로드 웹사이트
 - <http://www.google.com> 에서 Xming으로 검색
 - <http://sourceforge.net/projects/xming/>

- 설치 및 사용방법
 - 실행 파일 다운로드 후 설치
 - Xming 실행
 - Xwindows GUI 프로그램을 사용
하기 위해서는 먼저 실행 필수





- In Linux
 - Open terminal (to compile and run PROGRAM)
 - Use familiar editor : vi, emacs, gedit, etc.
- In Windows
 - Use SSH client : SecureShellClient, PuTTY, etc.
 - IP : xxx.xxx.xxx.xxx Port : xx
 - Login ID : password :
 - notepad++





Checking Environment



➤ Move to debugging and computing node

- Use **ssh**
- Usage : ssh s000#
- ex) ssh s0001

```
[edun20@master01 ~]$ ssh s0001
Last login: Thu Aug 30 13:33:46 2012 from master01
[edun20@s0001 ~]$ hostname
s0001
[edun20@s0001 ~]$
```

➤ Compiler Environment

- Use **module** command
- Usage : module add compiler/gcc-4.4.6

```
[edun20@s0001 ~]$ module availble
----- /applic/Modules/modulefiles -----
(module list) ...
[edun20@s0001 ~]$ module add compiler/gcc-4.4.6
[edun20@s0001 ~]$ module list
Currently Loaded Modulefiles:
  1) compiler/gcc-4.4.6
```



Checking Environment



Fortran	C
<pre>PROGRAM hello_world !\$omp parallel PRINT *, 'Hello World' !\$omp end parallel END</pre>	<pre>#include <stdio.h> int main() { #pragma omp parallel { printf ("Hello World\n"); } return 0; }</pre>
<pre>\$ gfortran -o hello.x hello.f90 \$ gfortran -fopenmp -o hello_omp.x hello.f90 \$./hello.x \$./hello_omp.x</pre>	<pre>\$ gcc -o hello.x hello.c \$ gcc -fopenmp -o hello_omp.x hello.c \$./hello.x \$./hello_omp.x</pre>
<pre>Intel : ifort -o hello.x hello.f90 GCC : gfortran -o hello.x hello.f90 PGI : pgf90 -o hello.x hello.f90</pre>	<pre>Intel : icc -o hello.x hello.c GCC : gcc -o hello.x hello.c PGI : pgcc -o hello.x hello.c</pre>
<pre>Intel : ifort -openmp -o hello_omp.x hello.f90 GCC : gfortran -fopenmp -o hello_omp.x hello.f90 PGI : pgf90 -mp -o hello_omp.x hello.f90</pre>	<pre>Intel : icc -openmp -o hello_omp.x hello.c GCC : gcc -fopenmp -o hello_omp.x hello.c PGI : pgcc -mp -o hello_omp.x hello.c</pre>

for output filename

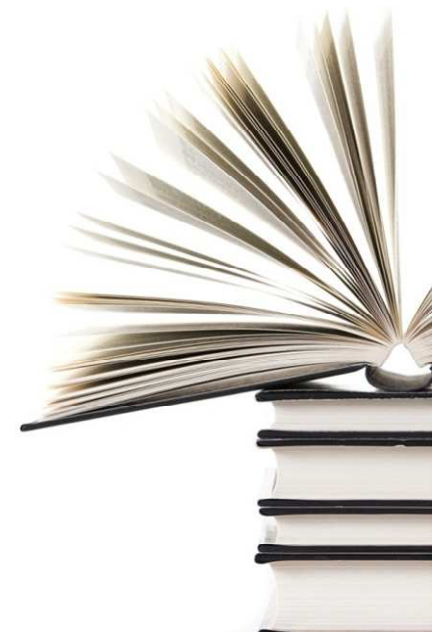
for output filename

for OpenMP

for OpenMP

Brief Review

1. OpenMP Basics Review



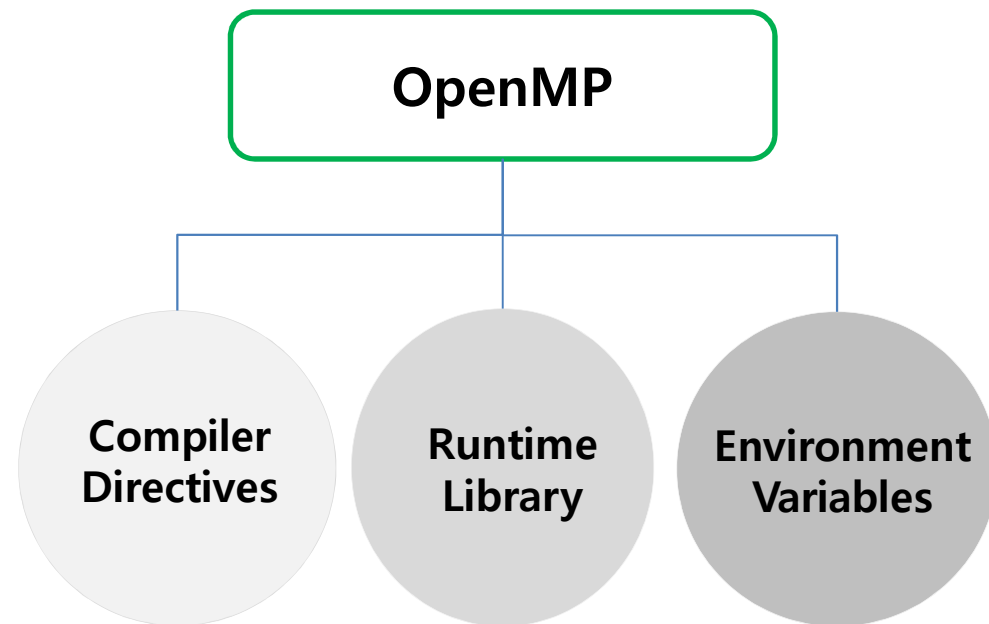


What is OpenMP ?



- OpenMP is
 - De-facto standard API (Application PROGRAMming Interface) for **multi-thread** based **shared memory** parallel PROGRAMming
 - **Not** a new PROGRAMming language
 - **Notation** that can be added to a sequential PROGRAM in C, C++ and Fortran

- Consists of
 - Compiler Directives
 - Runtime Library
 - Environment Variables





Creating Threads



Fortran	C
<pre>PROGRAM HELLO IMPLICIT NONE INTEGER omp_get_thread_num CALL omp_set_num_threads(4) !\$omp parallel PRINT *, 'Hello World', omp_get_thread_num() !\$omp end parallel END</pre>	<pre>#include <stdio.h> #include <omp.h> int main() { omp_set_num_threads(4); #pragma omp parallel num_threads(4) { printf ("Hello World %d\n", omp_get_thread_num()); } return 0; }</pre>
<pre>\$ export OMP_NUM_THREADS=4 (ksh/bash) \$ setenv OMP_NUM_THREADS 4 (csh) Intel : ifort -openmp -o hello.x hello.f90 GCC : gfortran -fopenmp -o hello.x hello.f90 PGI : pgf90 -mp -o hello.x hello.f90</pre>	<pre>\$ export OMP_NUM_THREADS=4 (ksh/bash) \$ setenv OMP_NUM_THREADS 4 (csh) Intel : icc -openmp -o hello.x hello.c GCC : gcc -fopenmp -o hello.x hello.c PGI : pgcc -mp -o hello.x hello.c</pre>



Data Scope Attribute



Fortran	C
<pre> PROGRAM PRIVATE_KEYWORD IMPLICIT NONE INTEGER tid, omp_get_thread_num INTEGER :: i = 10 CALL omp_set_num_threads(4) !\$omp parallel private(tid) firstprivate(i) tid = omp_get_thread_num() PRINT *, 'Hello World ', 'tid=', tid, ' i=', i !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int tid, i=10; omp_set_num_threads(4); #pragma omp parallel private(tid) firstprivate(i) { tid = omp_get_thread_num(); printf ("Hello World tid = %d i= %d\n", tid, i); } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o private_keyword.x private_keyword.f90 \$./private_keyword.x </pre>	<pre> \$ gcc -fopenmp -o private_keyword.x private_keyword.c \$./private_keyword.x </pre>



Synchronization



Fortran	C
<pre> PROGRAM SYNC_REVIEW IMPLICIT NONE INTEGER, PARAMETER :: N=2000000 INTEGER(8) :: i, sum=0 INTEGER, DIMENSION(0:N-1) :: A, B DO i=0, N-1 A(i) = i+1 B(i) = i+2 ENDDO CALL omp_set_num_threads(4) !\$omp parallel !\$OMP DO DO i=0, N-1 !\$OMP ATOMIC sum = sum + A(i) * B(i) END DO !\$omp end parallel PRINT *, "sum =", sum END </pre>	<pre> #include <stdio.h> #include <omp.h> #define N 2000000 int main() { long i, sum=0; int a[N], b[N]; for (i=0; i<N; i++) { a[i] = i+1; b[i] = i+2; } omp_set_num_threads(4); #pragma omp parallel { #pragma omp for for (i=0; i<N; i++) #pragma omp atomic sum += a[i] * b[i]; } printf("sum = %ld\n", sum); return 0; } </pre>
<pre> \$ gfortran -fopenmp -o sync_review.x sync_review.f90 \$ ulimit -s 512000 \$./sync_review.x </pre>	<pre> \$ gcc -fopenmp -o sync_review.x sync_review.c \$ ulimit -s 512000 \$./sync_review.x </pre>



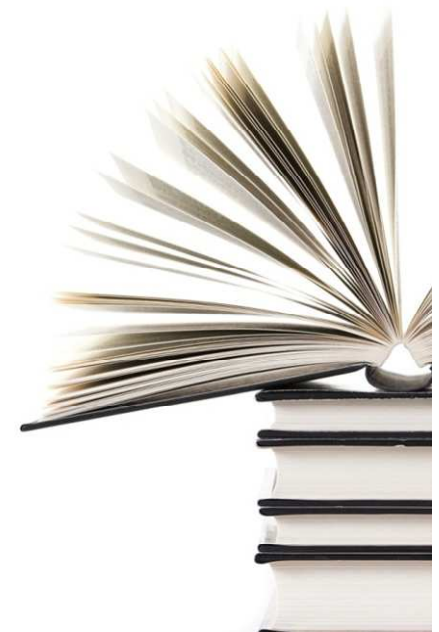
Reduction



Fortran	C
<pre> PROGRAM REDUCTION_REVIEW IMPLICIT NONE INTEGER, PARAMETER :: N=2000000 INTEGER(8) :: i, sum=0 INTEGER, DIMENSION(0:N-1) :: A, B DO i=0, N-1 A(i) = i+1 B(i) = i+2 ENDDO CALL omp_set_num_threads(4) !\$omp parallel DO reduction(+:sum) DO i=0, N-1 sum = sum + A(i) * B(i) END DO !\$omp end parallel DO PRINT *, "sum =", sum END </pre>	<pre> #include <stdio.h> #include <omp.h> #define N 2000000 int main() { long i, sum=0; int a[N], b[N]; for(i=0; i<N; i++) { a[i] = i+1; b[i] = i+2; } omp_set_num_threads(4); #pragma omp parallel for reduction (+:sum) for(i=0; i<N; i++) sum += a[i] * b[i]; printf("sum = %ld\n", sum); return 0; } </pre>
<pre> \$ gfortran -fopenmp -o reduce_review.x reduce_review.f90 \$ ulimit -s 512000 \$./reduce_review.x </pre>	<pre> \$ gcc -fopenmp -o reduce_review.x reduce_review.c \$ ulimit -s 512000 \$./reduce_review.x </pre>

Create Threads

1. Nested Parallel





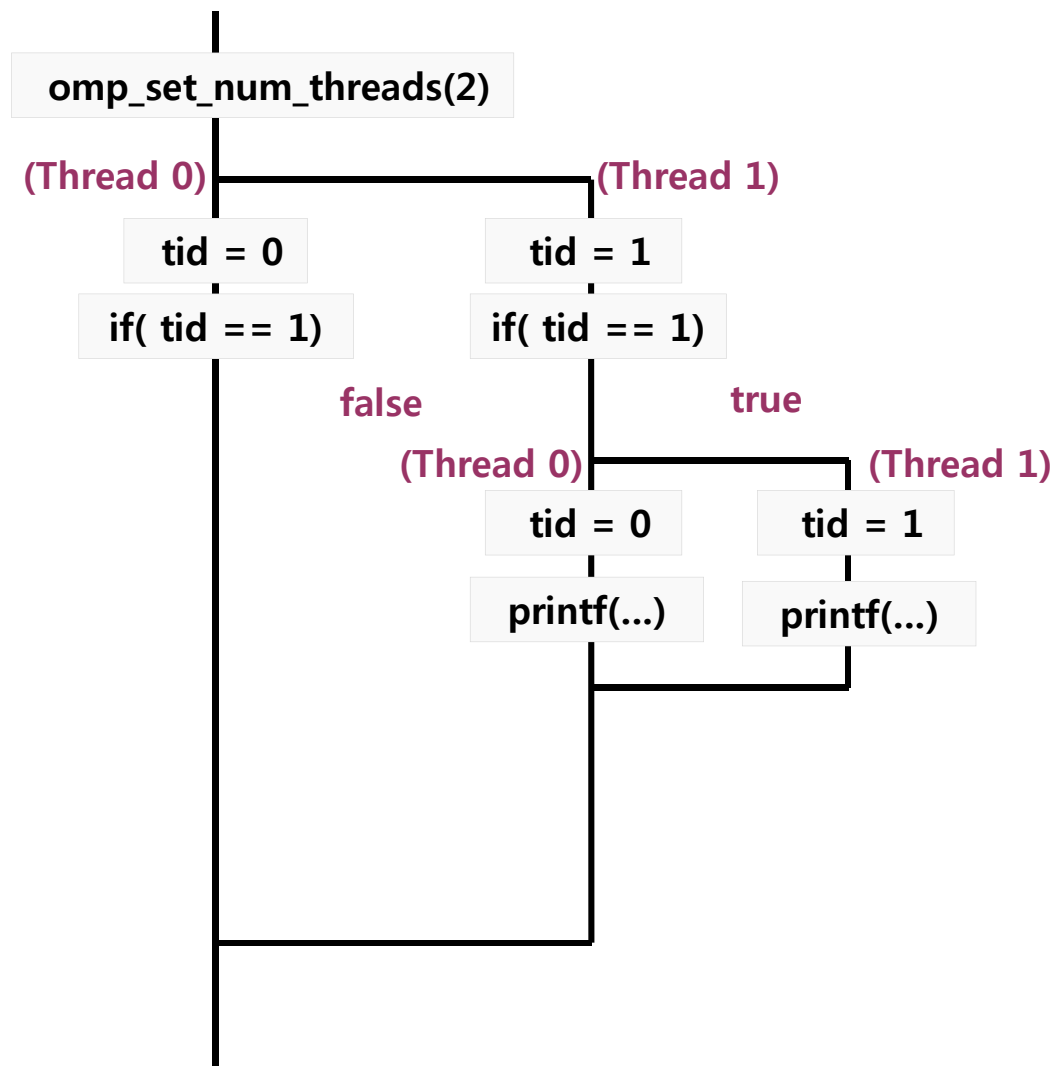
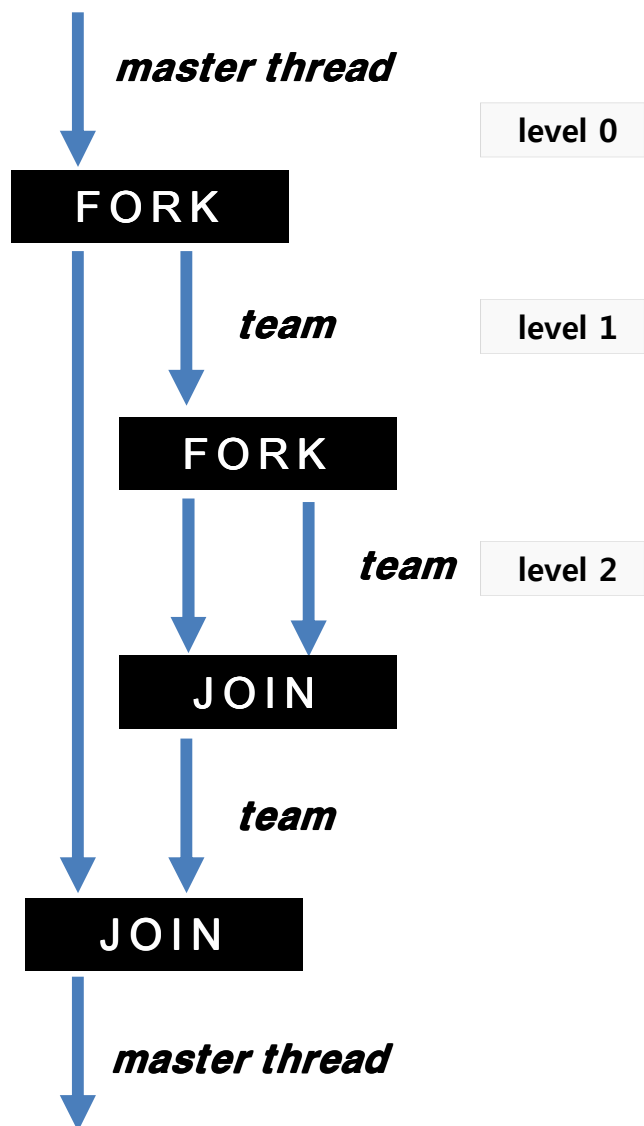
Create Threads : Nested Parallel (1/3)



Fortran	C
<pre> PROGRAM nested_parallel INTEGER tid, omp_get_thread_num CALL omp_set_nested(1) CALL omp_set_num_threads(2) !\$omp parallel private(tid) tid = omp_get_thread_num() PRINT 10, 'thread id =', tid IF(tid == 1) THEN !\$omp parallel private(tid) tid = omp_get_thread_num() print 20, 'thread id =', tid !\$omp end parallel END IF !\$omp end parallel 10 FORMAT(A,I4) 20 FORMAT(T8,A,I4) END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int tid; omp_set_nested(1); omp_set_num_threads(2); #pragma omp parallel private(tid) { tid = omp_get_thread_num(); printf("thread id=%d\n", tid); if(tid == 1) { #pragma omp parallel private(tid) { tid = omp_get_thread_num(); printf("\t thread id=%d\n", tid); } } } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o nested_parallel.x nested_parallel.f90 \$./ nested_parallel.x </pre>	<pre> \$ gcc -fopenmp -o nested_parallel.x nested_parallel.c \$./ nested_parallel.x </pre>

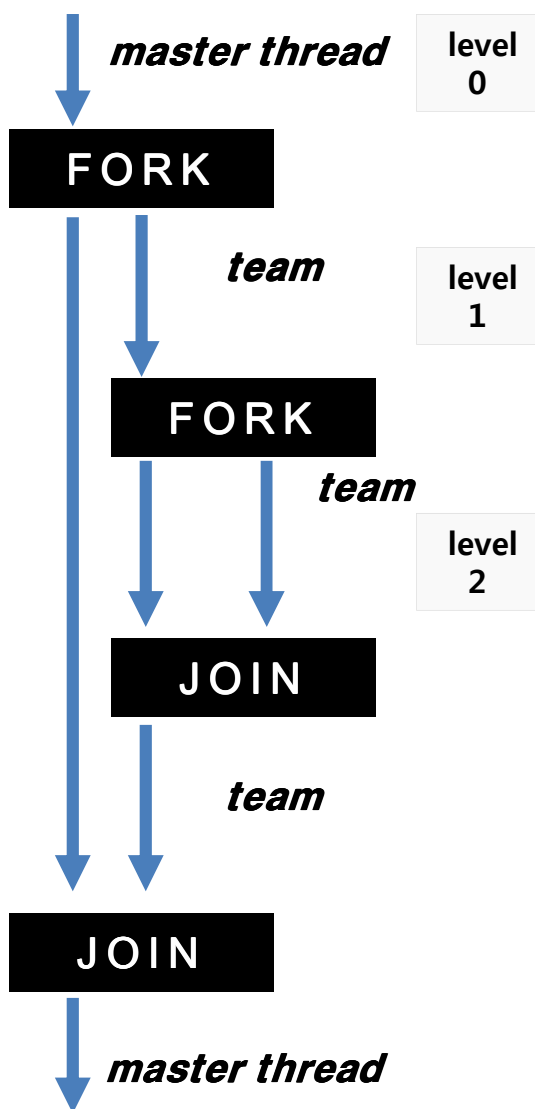


Create Threads : Nested Parallel (2/3)





Create Threads : Nested Parallel (2/3)



Fortran	C
omp_set_nested(nested) enables or disables nested parallelism	omp_set_nested(int nested) enables or disables nested parallelism
omp_get_nested() the value of the nes-var IVC	omp_get_nested() the value of the nes-var ICV
omp_get_level() the number of nested parallel regions	omp_get_level() the number of nested parallel regions
omp_get_active_level() the number of nested, active parallel regions	omp_get_active_level() the number of nested, active parallel regions
omp_get_ancestor_thread_num(level) the thread number of the ancestor or the current thread	omp_get_ancestor_thread_num(int level) the thread number of the ancestor or the current thread
omp_get_team_size(level) the size of the thread team	omp_get_team_size(int level) the size of the thread team



Create Threads : Nested Parallel (3/3)



Fortran	C
<pre> PROGRAM more_nested_para INTEGER tid, level INTEGER omp_get_thread_num INTEGER omp_get_level INTEGER omp_get_ancestor_thread_num CALL omp_set_nested(.true.) CALL omp_set_num_threads(4) !\$omp parallel private(tid, level) tid = omp_get_thread_num() level = omp_get_level() PRINT 10, 'thread id =', tid IF (tid == 1) THEN !\$omp parallel private(tid) num_threads(tid+2) tid = omp_get_thread_num() PRINT 20, 'thread id =', tid, ' ancestor_thread_num(', & level, ')=', omp_get_ancestor_thread_num(level) !\$omp end parallel END IF !\$omp end parallel 10 FORMAT(A,I4) 20 FORMAT(T8,A,I4,A,I4,A,I4) END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int tid, level; omp_set_nested(1); omp_set_num_threads(4); #pragma omp parallel private(tid, level) { tid = omp_get_thread_num(); level = omp_get_level(); printf("tid=%d level=%d\n", tid, level); if(tid == 1) { #pragma omp parallel private(tid) num_threads(tid+2) { tid = omp_get_thread_num(); printf("\t tid=%d ancestor_thread_num(%d)=%d\n", tid, level, omp_get_ancestor_thread_num(level)); } } } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o more_nested_para.x more_nested_para.f90 \$./more_nested_para.x </pre>	<pre> \$ gcc -fopenmp -o more_nested_para.x more_nested_para.c \$./more_nested_para.x </pre>



Nested Parallel : Data Scope (1/3)



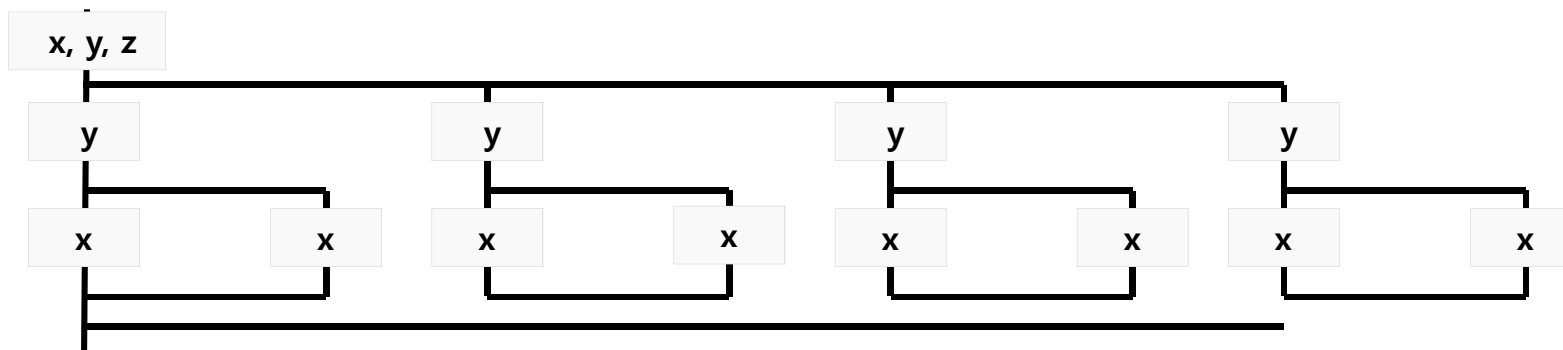
Fortran	C
<pre>PROGRAM nested_parallel_data_scope INTEGER x, y, z CALL omp_set_nested(1) CALL set_num_threads(4) !\$omp parallel private(y) x, y, z private? Shared? !\$omp parallel num_threads(2) private(x) x, y, z private? shared? !\$omp end parallel !\$omp end parallel END PROGRAM</pre>	<pre>int main() { int x, y, z; omp_set_nested(1); omp_set_num_threads(4); #pragma omp parallel private(y) { x,y,z private? shared? #pragma omp parallel num_threads(2) private(x) { x,y,z private? shared? } } return 0; }</pre>



Nested Parallel : Data Scope (2/3)



Fortran	C
<pre>PROGRAM nested_parallel_data_scope INTEGER x, y, z CALL omp_set_nested(1) CALL set_num_threads(4) !\$omp parallel private(y) x : shared y : private z : shared !\$omp parallel num_threads(2) private(x) x : private y : shared z : shared !\$omp end parallel !\$omp end parallel END PROGRAM</pre>	<pre>int main() { int x, y, z; omp_set_nested(1); omp_set_num_threads(4); #pragma omp parallel private(y) { x : shared y : private z : shared #pragma omp parallel num_threads(2) private(x) { x : private y : shared z : shared } } return 0; }</pre>





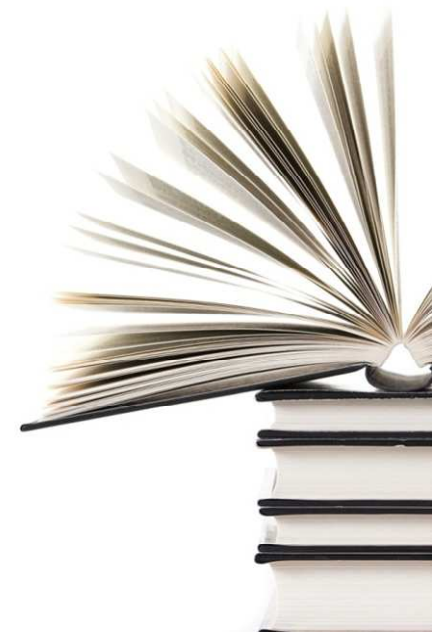
Nested Parallel : Data Scope (3/3)



Fortran	C
<pre> PROGRAM nested_parallel_data_scope INTEGER :: x=1, y=10, z=20, tid INTEGER omp_get_thread_num CALL omp_set_nested(.true.) CALL omp_set_num_threads(4) !\$omp parallel private(y, tid) tid = omp_get_thread_num() x = x + 1; y = 12; z = 22 !\$omp parallel num_threads(2) private(x,tid) tid = omp_get_thread_num() x = 10; y = y + 1; z = z + 1 PRINT 30, 'tid =', tid, ' x =', x, ' y=', y, ' z=', z !\$omp end parallel PRINT 20, 'tid =', tid, ' x =', x, ' y=', y, ' z=', z !\$omp end parallel PRINT 10, ' x =', x, ' y=', y, ' z=', z 10 FORMAT(A,I4,A,I4,A,I4) 20 FORMAT(A,I4,A,I4,A,I4,A,I4) 30 FORMAT(T8,A,I4,A,I4,A,I4,A,I4) END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int x=1, y=10, z=20, tid; omp_set_nested(1); omp_set_num_threads(4); #pragma omp parallel private(y, tid) { tid = omp_get_thread_num(); x++; y = 12; z = 22; #pragma omp parallel num_threads(2) private(x, tid) { tid = omp_get_thread_num(); x = 10; y++; z++; printf("\ttid=%d x=%d y=%d z=%d\n", tid, x, y, z); } printf("tid=%d x=%d y=%d z=%d\n", tid, x, y, z); } printf("x=%d y=%d z=%d\n", x, y, z); return 0; } </pre>
<pre> \$ gfortran -fopenmp -o nested_parallel_ds.x nested_parallel_ds.f90 \$./nested_parallel_ds.x </pre>	<pre> \$ gcc -fopenmp -o nested_parallel_ds.x nested_parallel_ds.c \$./nested_parallel_ds.x </pre>

Work Sharing

- 1. Sections**
- 2. Single**
- 3. master**





Work-Share Constructs



➤ Types of Work-Sharing Constructs

- **do/for**
- **sections**
- **single**
- **workshare**

- Work-Sharing construct divides the execution of the enclosed code region among members of the team encounter it
- Work-Sharing constructs **do not launch new threads**
- There is no implied barrier upon entry to a work-sharing construct, however there is an implied barrier at the END of a work sharing construct.
- workshare construct is only The Fortran



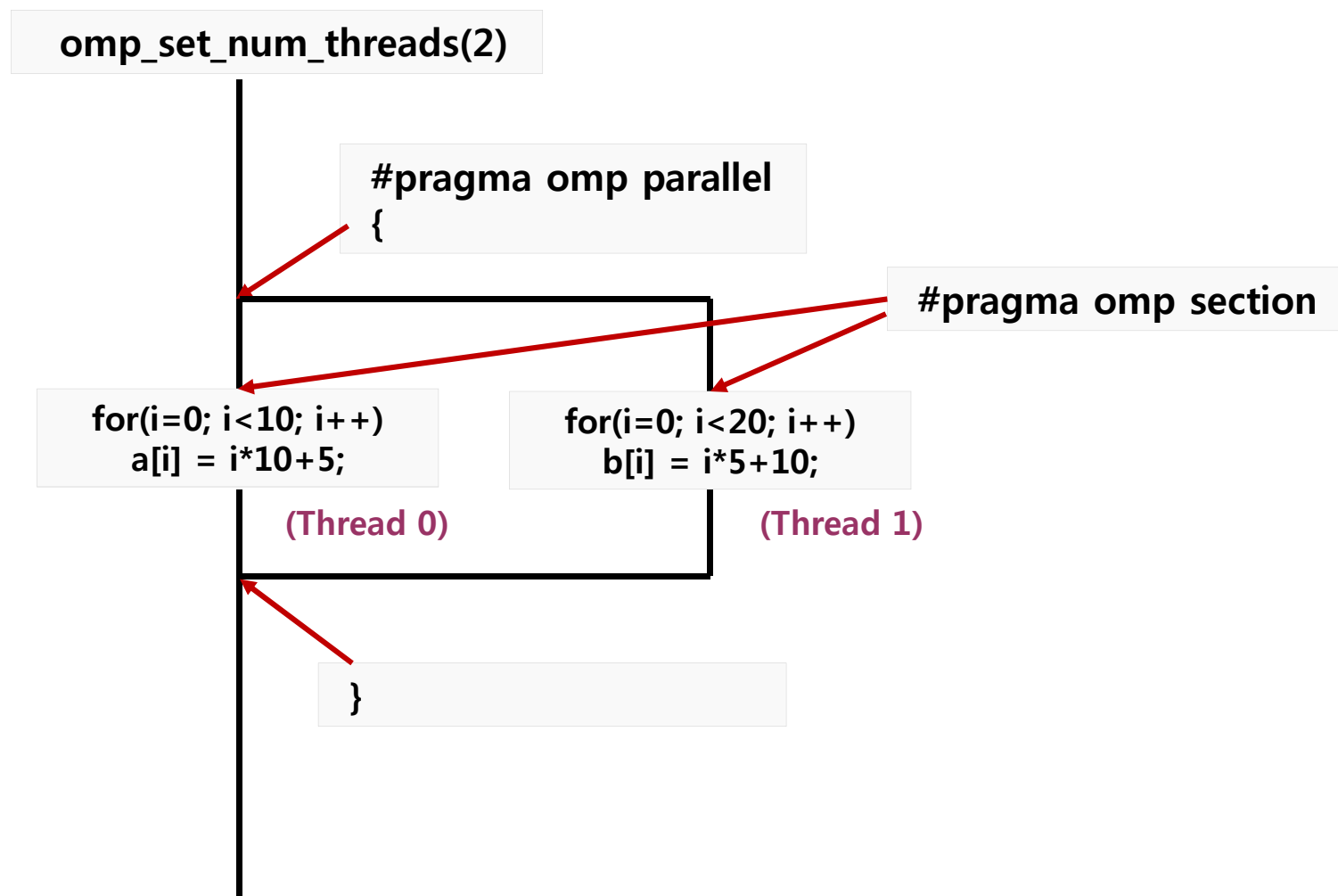
Work-Share Constructs : Sections



Fortran	C
<pre> PROGRAM SECTIONS IMPLICIT NONE INTEGER i, a(0:9), b(0:19) CALL omp_set_num_threads(2) !\$omp parallel !\$omp sections !\$omp section do i=0, 9 a(i) = i * 10 + 5 END DO !\$omp section do i=0, 19 b(i) = i * 5 + 10 END DO !\$omp end sections !\$omp end parallel WRITE(*,10) a WRITE(*,20) b 10 FORMAT(10i4) 20 FORMAT(20i4) END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int i, a[10], b[20]; omp_set_num_threads(2); #pragma omp parallel private(i) { #pragma omp sections { #pragma omp section for (i=0; i<10; i++) a[i] = i * 10 + 5; #pragma omp section for (i=0; i<20; i++) b[i] = i * 5 + 10; } for(i=0; i<10; i++) printf("%d ", a[i]); printf("\n"); for (i=0; i<20; i++) printf("%d ", b[i]); printf("\n"); return 0; } } </pre>
<pre> \$ gfortran -fopenmp -o sections.x sections.f90 \$./sections.x </pre>	<pre> \$ gcc -fopenmp -o sections.x sections.c \$./sections.x </pre>



Work-Share Constructs : Sections





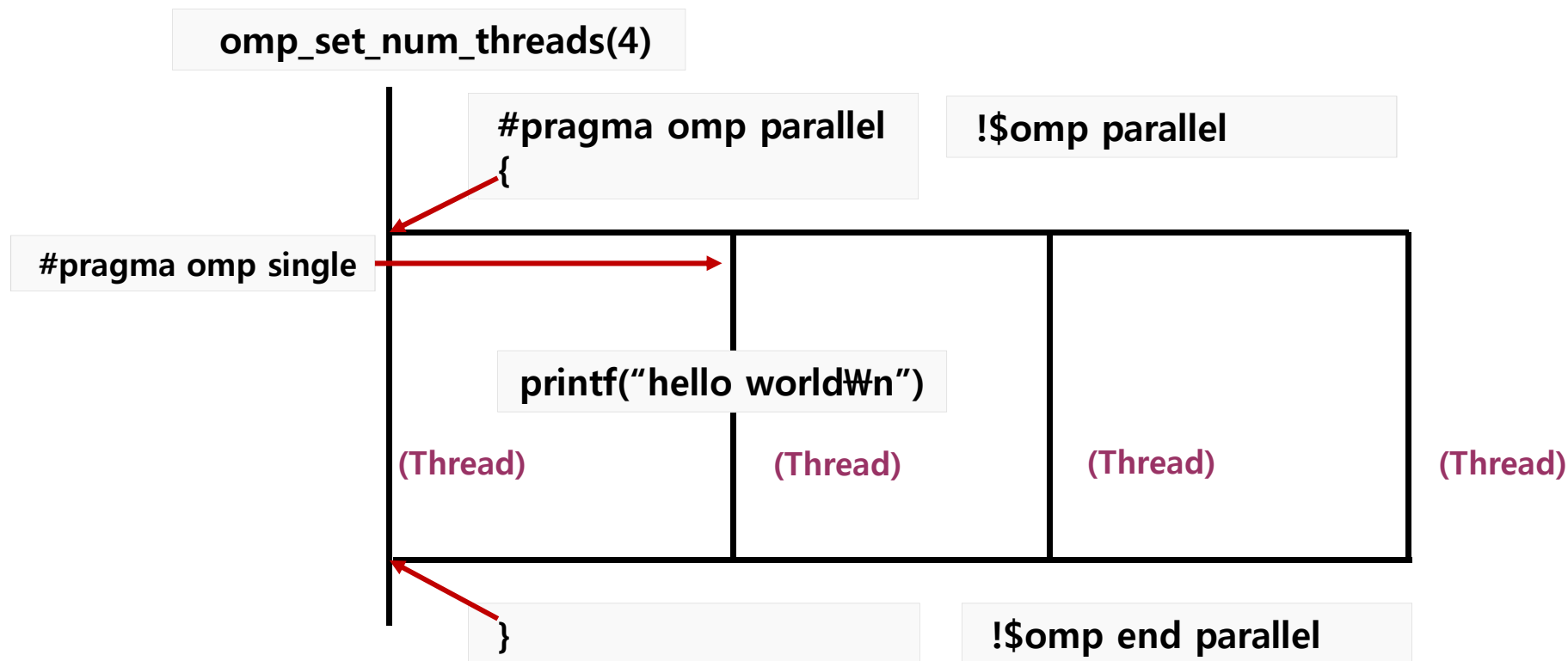
Work-Share Constructs : Single



Fortran	C
<pre>PROGRAM SINGLE IMPLICIT NONE CALL omp_set_num_threads(4) !\$omp parallel !\$omp single PRINT *, 'Hello World' !\$omp end single !\$omp end parallel END</pre>	<pre>#include <stdio.h> #include <omp.h> int main() { omp_set_num_threads(4); #pragma omp parallel { #pragma omp single { printf("Hello world\n"); } } return 0; }</pre>
<pre>\$ gfortran -fopenmp -o single.x single.f90 \$./single.x</pre>	<pre>\$ gcc -fopenmp -o single.x single.c \$./single.x</pre>



Work-Share Constructs : Single





Work-Share Constructs : master



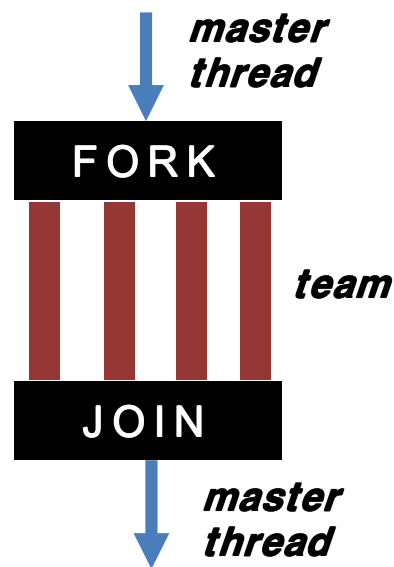
Fortran	C
<pre>PROGRAM MASTER IMPLICIT NONE INTEGER omp_get_thread_num CALL omp_set_num_threads(4) !\$omp parallel !\$omp master CALL sleep(1) PRINT *, 'Hello World' !\$omp end master PRINT *, 'tid=',omp_get_thread_num() !\$omp end parallel END</pre>	<pre>#include <stdio.h> #include <unistd.h> #include <omp.h> int main() { omp_set_num_threads(4); #pragma omp parallel { #pragma omp master { sleep(1); printf("hello world\n"); } printf("tid = %d\n", omp_get_thread_num()); } return 0; }</pre>
<pre>\$ gfortran -fopenmp -o master.x master.f90 \$./master.x</pre>	<pre>\$ gcc -fopenmp -o master.x master.c \$./master.x</pre>

➤ MASTER

- The MASTER directive specifies a region that is to be **executed only** by the **master thread of the threads**
- **All other threads** on the threads **skip this section** of code
- SINGLE on master thread
- There is **no implied barrier** associated with this directive

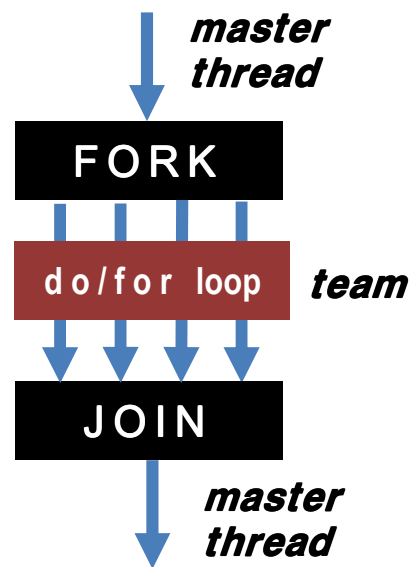


Work-Share Constructs



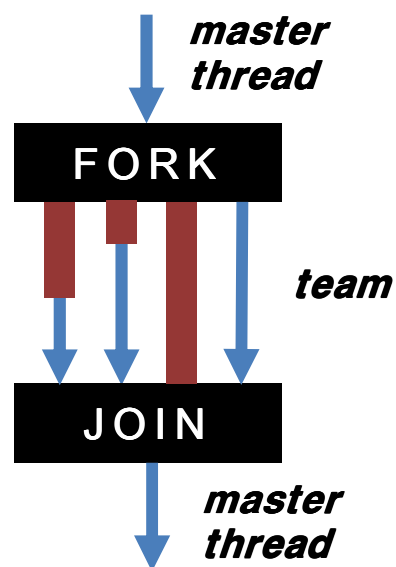
parallel

```
#pragma omp parallel
{
    [red bar]
}
```



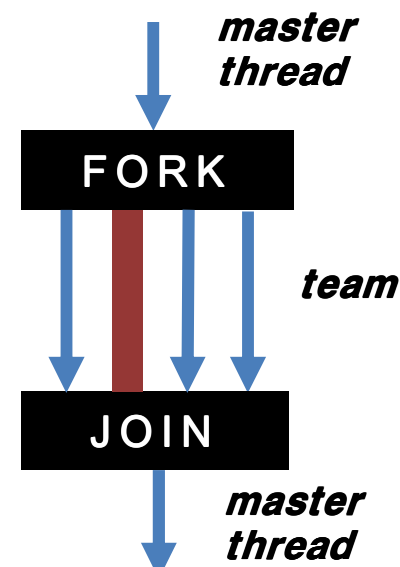
do/for

```
#pragma omp parallel
{
    #pragma omp for
    [red bar]
}
```



sections

```
#pragma omp parallel
{
    #pragma sections
    {
        #pragma omp section
        [red bar]
        #pragma omp section
        [red bar]
        #pragma omp section
        [red bar]
    }
}
```



single

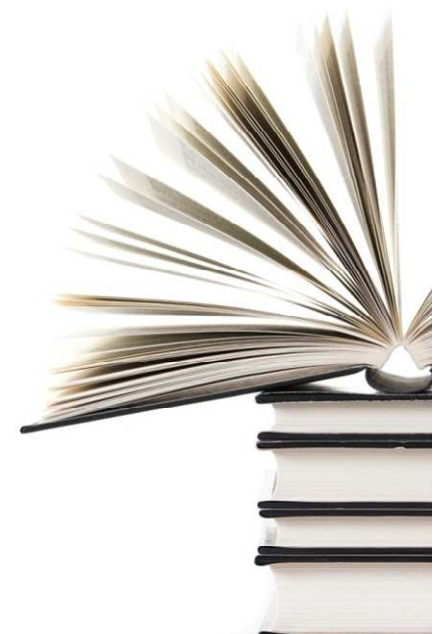
```
#pragma omp parallel
{
    #pragma omp single
    [red bar]
}
```

Break!!



Synchronization

1. **nowait**
2. **ordered/lock/flush**





Synchronization : nowait



Fortran	C
<pre>PROGRAM NOWAIT IMPLICIT NONE INTEGER :: x=1 CALL omp_set_num_threads(16) !\$omp parallel !\$OMP SINGLE x = x+1 PRINT *, 'x =', x !\$omp end SINGLE !\$omp SINGLE x = x+1 PRINT *, 'x =', x !\$omp end SINGLE !\$omp end parallel END</pre> \$./a.out x=2 x=3	<pre>#include <stdio.h> #include <omp.h> int main() { int x = 1; omp_set_num_threads(16); #pragma omp parallel { #pragma omp single { x++; printf("x=%d\n", x); } #pragma omp single { x++; printf("x=%d\n", x); } } return 0; }</pre> \$./a.out x=2 x=3
<pre>\$ gfortran -fopenmp -o nowait.x nowait.f90 \$./nowait.x</pre>	<pre>\$ gcc -fopenmp -o nowait.x nowait.c \$./nowait.x</pre>



Synchronization : nowait



Fortran	C
<pre>PROGRAM NOWAIT1 IMPLICIT NONE INTEGER :: x=1 CALL omp_set_num_threads(16) !\$omp parallel !\$OMP SINGLE x=x+1 print*, 'x =', x !\$omp end SINGLE nowait !\$OMP SINGLE x=x+1 print*, 'x =', x !\$omp end SINGLE !\$omp end parallel END</pre> What happen? <pre>\$./a.out x=2 x=3 \$./a.out x=3 x=2 \$./a.out x=3 x=3</pre>	<pre>#include <stdio.h> #include <omp.h> int main() { int x = 1; omp_set_num_threads(16); #pragma omp parallel { #pragma omp single nowait { x++; printf("x=%d\n", x); } #pragma omp single { x++; printf("x=%d\n", x); } } return 0; }</pre> What happen? <pre>\$./a.out x=2 x=3 \$./a.out x=3 x=2 \$./a.out x=3 x=3</pre>
<pre>\$ gfortran -fopenmp -o nowait1.x nowait1.f90 \$./nowait1.x</pre>	<pre>\$ gcc -fopenmp -o nowait1.x nowait1.c \$./nowait1.x</pre>



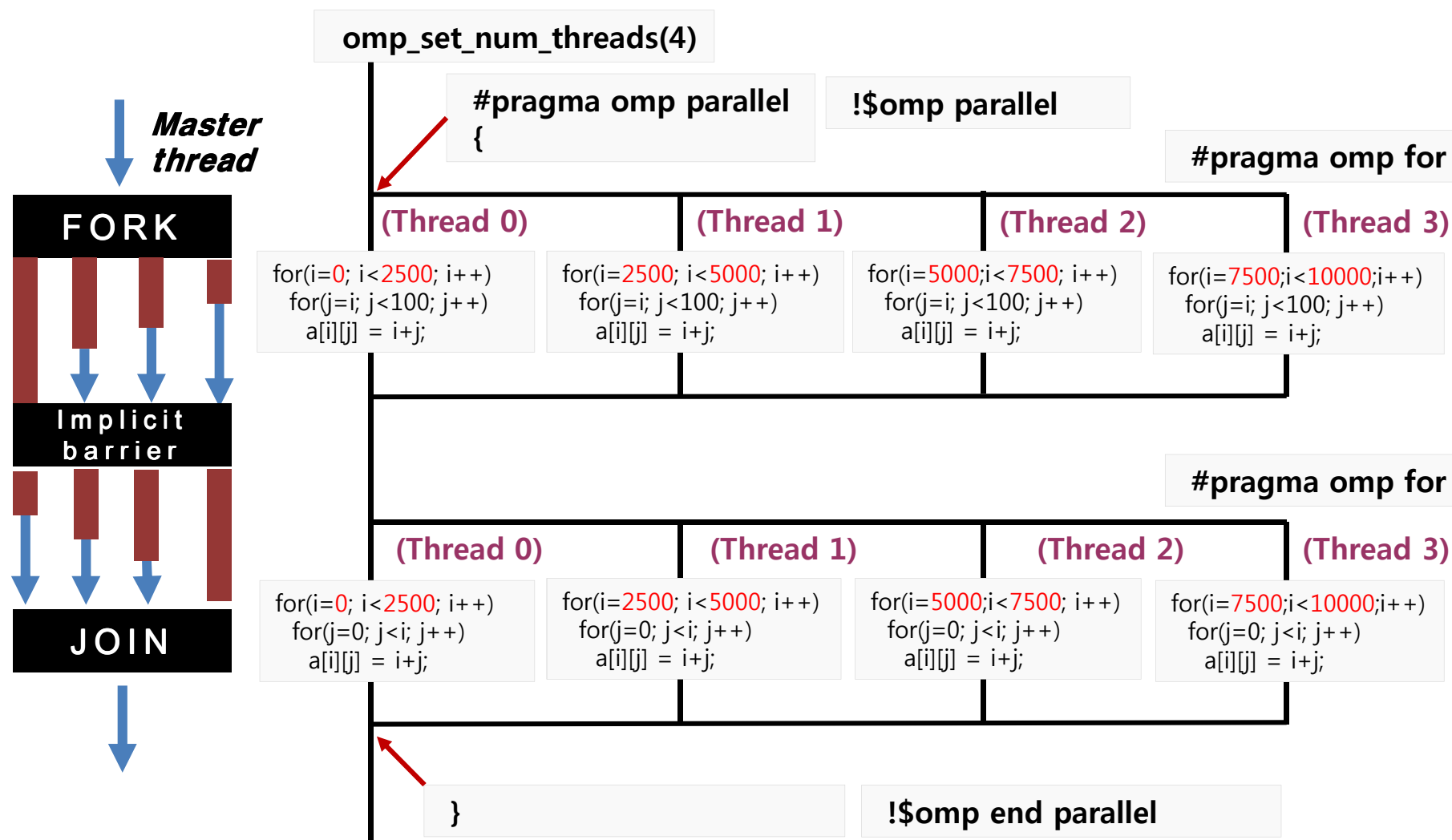
Synchronization : nowait



Fortran	C
<pre> PROGRAM NOWAIT_FOR IMPLICIT NONE INTEGER, PARAMETER :: N = 9999 INTEGER i, j, a(0:N, 0:N) CALL omp_set_num_threads(4) !\$omp parallel private(i,j) !\$omp do DO j=0, N DO i=0, j a(i,j) = i+j END DO END DO !\$omp do DO j=0, N DO i=j+1, N a(i,j) = i-j END DO END DO !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <omp.h> #define N 10000 int main() { int i, j, a[N][N]; omp_set_num_threads(4); #pragma omp parallel private(i, j) { #pragma omp for for(i=0; i<N; i++) for(j=i; j<N; j++) a[i][j] = i+j; #pragma omp for for(i=0; i<N; i++) for(j=0; j<i; j++) a[i][j] = i-j; } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o for_nowait_for.x nowait_for.f90 \$ ulimit -s 512000 \$ time ./nowait_for.x </pre>	<pre> \$ gcc -fopenmp -o nowait_for.x nowait_for.c \$ ulimit -s 512000 \$ time ./nowait_for.x </pre>



Synchronization : nowait





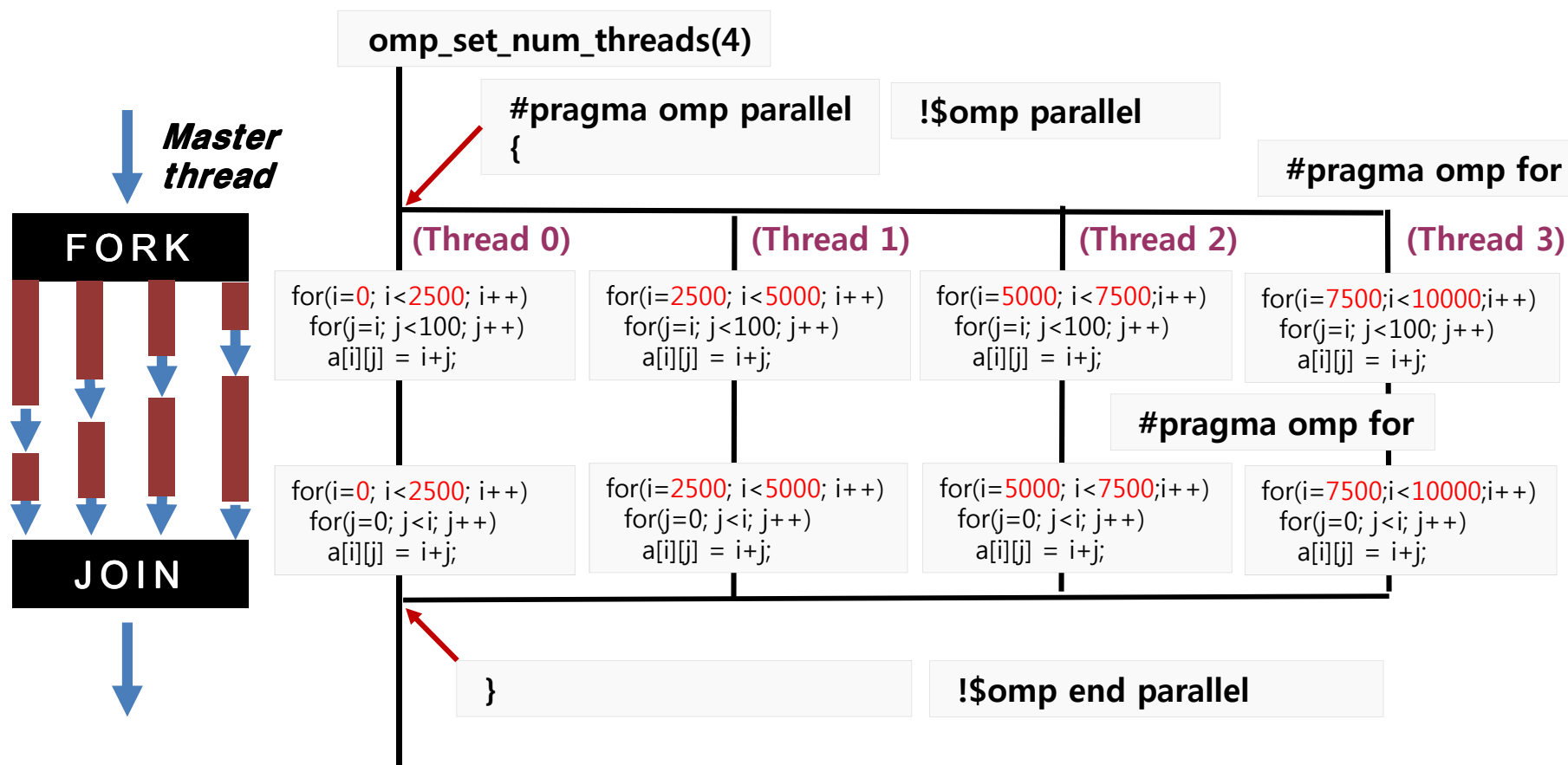
Synchronization : nowait



Fortran	C
<pre> PROGRAM nowait_for INTEGER, PARAMETER :: N = 9999 INTEGER i, j, a(0:N, 0:N) CALL omp_set_num_threads(4) !\$omp parallel private(i,j) !\$omp do DO j=0, N DO i=0, j a(i,j) = i+j END DO END DO !\$omp end DO nowait !\$omp do DO j=0, N DO i=j+1, N a(i,j) = i-j END DO END DO !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <omp.h> #define N 10000 int main() { int i, j, a[N][N]; omp_set_num_threads(4); #pragma omp parallel private(i, j) { #pragma omp for nowait for(i=0; i<N; i++) for(j=i; j<N; j++) a[i][j] = i+j; #pragma omp for for(i=0; i<N; i++) for(j=0; j<i; j++) a[i][j] = i-j; } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o for_nowait2.x nowait.f90 \$ ulimit -s 512000 \$ time ./for_nowait2.x </pre>	<pre> \$ gcc -fopenmp -o nowait_for2.x nowait_for2.c \$ ulimit -s 512000 \$ time ./nowait_for2.x </pre>



Synchronization : nowait





Synchronization : Simple Test (1/5)



Fortran	C
<pre> PROGRAM simple_test1 IMPLICIT NONE INTEGER, PARAMETER :: N = 20 INTEGER :: i, tid, a(N), omp_get_thread_num CALL omp_set_num_threads(4) !\$omp parallel private(tid) tid = omp_get_thread_num() IF (tid /= 2) THEN CALL sleep(2) END IF !\$OMP DO DO i=0, N-1 a(i) = i PRINT *, 'a(',i,') =',a(i),'tid =',tid END DO !\$omp end DO PRINT *, 'END', tid, ' thread' !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <unistd.h> #include <omp.h> #define N 20 int main() { int i, tid, a[N]; omp_set_num_threads(4); #pragma omp parallel private(tid) { tid = omp_get_thread_num(); if (tid != 2) sleep(2); #pragma omp for for (i=0; i<N; i++) { a[i] = i; printf("a[%d]=%d tid=%d\n", i, a[i], tid); } printf("END %d thread\n", tid); } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o simple_test1.x simple_test1.f90 \$./simple_test1.x </pre>	<pre> \$ gcc -fopenmp -o simple_test1.x simple_test1.c \$./simple_test1.x </pre>



Synchronization : Simple Test (2/5)



Fortran	C
<pre> PROGRAM simple_test2 IMPLICIT NONE INTEGER, PARAMETER :: N = 20 INTEGER :: i, tid, a(N), omp_get_thread_num CALL omp_set_num_threads(4) !\$omp parallel private(tid) tid = omp_get_thread_num() IF (tid /= 2) THEN CALL sleep(2) END IF !\$OMP DO DO i=0, N-1 a(i) = i PRINT *, 'a(',i,') =',a(i),'tid =',tid END DO !\$omp end DO nowait PRINT *, 'END', tid, ' thread' !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <unistd.h> #include <omp.h> #define N 20 int main() { int i, tid, a[N]; omp_set_num_threads(4); #pragma omp parallel private(tid) { tid = omp_get_thread_num(); if (tid != 2) sleep(2); #pragma omp for nowait for (i=0; i<N; i++) { a[i] = i; printf("a[%d]=%d tid=%d\n", i, a[i], tid); } printf("END %d thread\n", tid); } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o simple_test2.x simple_test2.f90 \$./simple_test2.x </pre>	<pre> \$ gcc -fopenmp -o simple_test2.x simple_test2.c \$./simple_test2.x </pre>



Synchronization : Simple Test (3/5)



Fortran	C
<pre> PROGRAM simple_test3 IMPLICIT NONE INTEGER, PARAMETER :: N = 4 INTEGER :: i, tid, omp_get_thread_num CALL omp_set_num_threads(4) !\$omp parallel private(i,tid) tid = omp_get_thread_num() IF (tid /= 2) THEN CALL sleep(2) END IF !\$OMP SECTIONS !\$OMP SECTION DO i=0, N-1 PRINT *, 'L1 tid =', tid END DO !\$OMP SECTION DO i=0, N-1 PRINT *, 'L2 tid =', tid END DO !\$omp end SECTIONS !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <unistd.h> #include <omp.h> #define N 4 int main() { int i, tid; omp_set_num_threads(4); #pragma omp parallel private(i,tid) { tid = omp_get_thread_num(); if(tid != 2) sleep(2); #pragma omp sections { #pragma omp section for (i=0; i<N; i++) printf("L1 tid=%d\n", tid); #pragma omp section for (i=0; i<N; i++) printf("L2 tid=%d\n", tid); } } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o simple_test3.x simple_test3.f90 \$./simple_test3.x </pre>	<pre> \$ gcc -fopenmp -o simple_test3.x simple_test3.c \$./simple_test3.x </pre>



Synchronization : Simple Test (4/5)



Fortran	C
<pre> PROGRAM simple_test4 IMPLICIT NONE INTEGER, PARAMETER :: N = 4 INTEGER :: i, tid, omp_get_thread_num CALL omp_set_num_threads(4) !\$omp parallel private(i,tid) tid = omp_get_thread_num() !\$OMP SECTIONS !\$OMP SECTION DO i=0, N-1 PRINT *, 'L1 tid =', tid END DO !\$OMP SECTION DO i=0, N-1 PRINT *, 'L2 tid =', tid END DO CALL sleep(2) !\$omp end SECTIONS PRINT *, 'tid=', tid !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <unistd.h> #include <omp.h> #define N 4 int main() { int i, tid; omp_set_num_threads(4); #pragma omp parallel private(i,tid) { tid = omp_get_thread_num(); #pragma omp sections { #pragma omp section for(i=0; i<N; i++) printf("L1 tid=%d\n", tid); #pragma omp section { for(i=0; i<N; i++) printf("L2 tid=%d\n", tid); sleep(2); } } printf("tid = %d\n", tid); } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o simple_test4.x simple_test4.f90 \$./simple_test4.x </pre>	<pre> \$ gcc -fopenmp -o simple_test4.x simple_test4.c \$./simple_test4.x </pre>



Synchronization : Simple Test (5/5)



Fortran	C
<pre> PROGRAM simple_test4 IMPLICIT NONE INTEGER, PARAMETER :: N = 4 INTEGER :: i, tid, omp_get_thread_num CALL omp_set_num_threads(4) !\$omp parallel private(i,tid) tid = omp_get_thread_num() !\$OMP SECTIONS !\$OMP SECTION DO i=0, N-1 PRINT *, 'L1 tid =', tid END DO !\$OMP SECTION DO i=0, N-1 PRINT *, 'L2 tid =', tid END DO CALL sleep(2) !\$omp end SECTIONS nowait PRINT *, 'tid=', tid !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <unistd.h> #include <omp.h> #define N 4 int main() { int i, tid; omp_set_num_threads(4); #pragma omp parallel private(i,tid) { tid = omp_get_thread_num(); #pragma omp sections nowait { #pragma omp section for(i=0; i<N; i++) printf("L1 tid=%d\n", tid); #pragma omp section { for(i=0; i<N; i++) printf("L2 tid=%d\n", tid); sleep(2); } } printf("tid = %d\n", tid); } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o simple_test5.x simple_test5.f90 \$./simple_test5.x </pre>	<pre> \$ gcc -fopenmp -o simple_test5.x simple_test5.c \$./simple_test5.x </pre>



Synchronization : ordered



Fortran	C
<pre> PROGRAM ordered IMPLICIT NONE INTEGER i, a(0:9) CALL omp_set_num_threads(4) !\$omp parallel private(i) !\$OMP DO ordered DO i=0, 9 a(i) = i * 2 !\$OMP ORDERED PRINT *, 'a(', i, ') = ', a(i) !\$omp end ORDERED END DO !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int i, a[10]; omp_set_num_threads(4); #pragma omp parallel private(i) { #pragma omp for ordered for(i=0; i<10; i++) { a[i] = i * 2; #pragma omp ordered printf("a[%d] = %d\n", i, a[i]); } } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o ordered.x ordered.f90 \$./ordered.x </pre>	<pre> \$ gcc -fopenmp -o ordered.x ordered.c \$./ordered.x </pre>

➤ ORDERED

- For pipelining loop iterations
- Can exist only in the dynamic extent of a DO or PARALLEL DO directive
- The DO directive to which it binds must have the ORDERED clause specified
- Only one thread can enter at a time



Synchronization : lock



Fortran	C
<pre> PROGRAM lock IMPLICIT NONE INTEGER, PARAMETER :: OMP_LOCK_KIND=8 INTEGER :: x=1 INTEGER(kind=OMP_LOCK_KIND) LCK CALL OMP_INIT_LOCK (LCK) CALL omp_set_num_threads(4) !\$omp parallel CALL omp_set_lock(LCK) x = x+1 PRINT *, 'x =', x CALL omp_unset_lock(LCK) !\$omp end parallel CALL omp_destroy_lock(LCK) END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int x = 1; omp_lock_t lock; omp_init_lock(&lock); omp_set_num_threads(4); #pragma omp parallel { omp_set_lock(&lock); x++; printf("x=%d\n", x); omp_unset_lock(&lock); } omp_destroy_lock(&lock); return 0; } </pre>
<pre> \$ gfortran -fopenmp -o lock.x lock.f90 \$./lock.x </pre>	<pre> \$ gcc -fopenmp -o lock.x lock.c \$./lock.x </pre>

mutually exclusive region

mutually exclusive region

Task

1. **task**
2. **taskwait**





Task (1/2)



Fortran	C
<pre>PROGRAM task1 IMPLICIT NONE !\$omp parallel num_threads(32) WRITE(*, '(A)', advance="no") 'A ' WRITE(*, '(A)', advance="no") 'B ' WRITE(*, '(A)', advance="no") 'C ' WRITE(*, '(A)', advance="no") 'D ' WRITE(*, *) ' ' !\$omp end parallel END</pre>	<pre>#include <stdio.h> #include <omp.h> int main() { #pragma omp parallel num_threads(32) { printf("A "); printf("B "); printf("C "); printf("D "); printf("\n"); } return 0; }</pre>
<pre>\$ gfortran -fopenmp -o task1.x task1.f90 \$./task1.x</pre>	<pre>\$ gcc -fopenmp -o task1.x task1.c \$./task1.x</pre>



Task (1/2)



Fortran	C
<pre>PROGRAM task2 IMPLICIT NONE INTEGER omp_get_thread_num !\$omp parallel num_threads(32) !\$OMP SINGLE PRINT *, 'A tid =', omp_get_thread_num() PRINT *, 'B tid =', omp_get_thread_num() PRINT *, 'C tid =', omp_get_thread_num() PRINT *, 'D tid =', omp_get_thread_num() !\$omp end SINGLE !\$omp end parallel END</pre>	<pre>#include <stdio.h> #include <omp.h> int main() { #pragma omp parallel num_threads(32) { #pragma omp single { printf("A tid=%d\n", omp_get_thread_num()); printf("B tid=%d\n", omp_get_thread_num()); printf("C tid=%d\n", omp_get_thread_num()); printf("D tid=%d\n", omp_get_thread_num()); } } return 0; }</pre>
<pre>\$ gfortran -fopenmp -o task2.x task2.f90 \$./task2.x</pre>	<pre>\$ gcc -fopenmp -o task2.x task2.c \$./task2.x</pre>



Task (1/2)



Fortran	C
<pre>PROGRAM task3 IMPLICIT NONE INTEGER omp_get_thread_num !\$omp parallel num_threads(32) !\$OMP SINGLE PRINT *, 'A tid =', omp_get_thread_num() !\$OMP TASK PRINT *, 'B tid =', omp_get_thread_num() !\$omp end TASK !\$OMP TASK PRINT *, 'C tid =', omp_get_thread_num() !\$omp end TASK PRINT *, 'D tid =', omp_get_thread_num() !\$omp end SINGLE !\$omp end parallel END</pre>	<pre>#include <stdio.h> #include <omp.h> int main() { #pragma omp parallel num_threads(32) { #pragma omp single { printf("A tid=%d\n", omp_get_thread_num()); #pragma omp task { printf("B tid=%d\n", omp_get_thread_num()); } #pragma omp task { printf("C tid=%d\n", omp_get_thread_num()); } printf("D tid=%d\n", omp_get_thread_num()); } } return 0; }</pre>
<pre>\$ gfortran -fopenmp -o task3.x task3.f90 \$./task3.x</pre>	<pre>\$ gcc -fopenmp -o task3.x task3.c \$./task3.x</pre>



Task (1/2)



Fortran	C
<pre> PROGRAM task3 IMPLICIT NONE INTEGER, PARAMETER :: N = 20 INTEGER :: i, omp_get_thread_num !\$omp parallel num_threads(8) !\$OMP SINGLE firstprivate(i) do while (i < N) !\$OMP TASK PRINT *, 'index : ', i, 'tid : ', omp_get_thread_num() !\$omp end TASK end do !\$omp end SINGLE !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <omp.h> #define N 20 int main() { #pragma omp parallel num_threads(8) { #pragma omp single { int i = 0; while (i++ < N) #pragma omp task { printf("index : %d, tid : %d \n", i, omp_get_thread_num()); } } } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o task4.x task4.f90 \$./task3.x </pre>	<pre> \$ gcc -fopenmp -o task4.x task4.c \$./task3.x </pre>

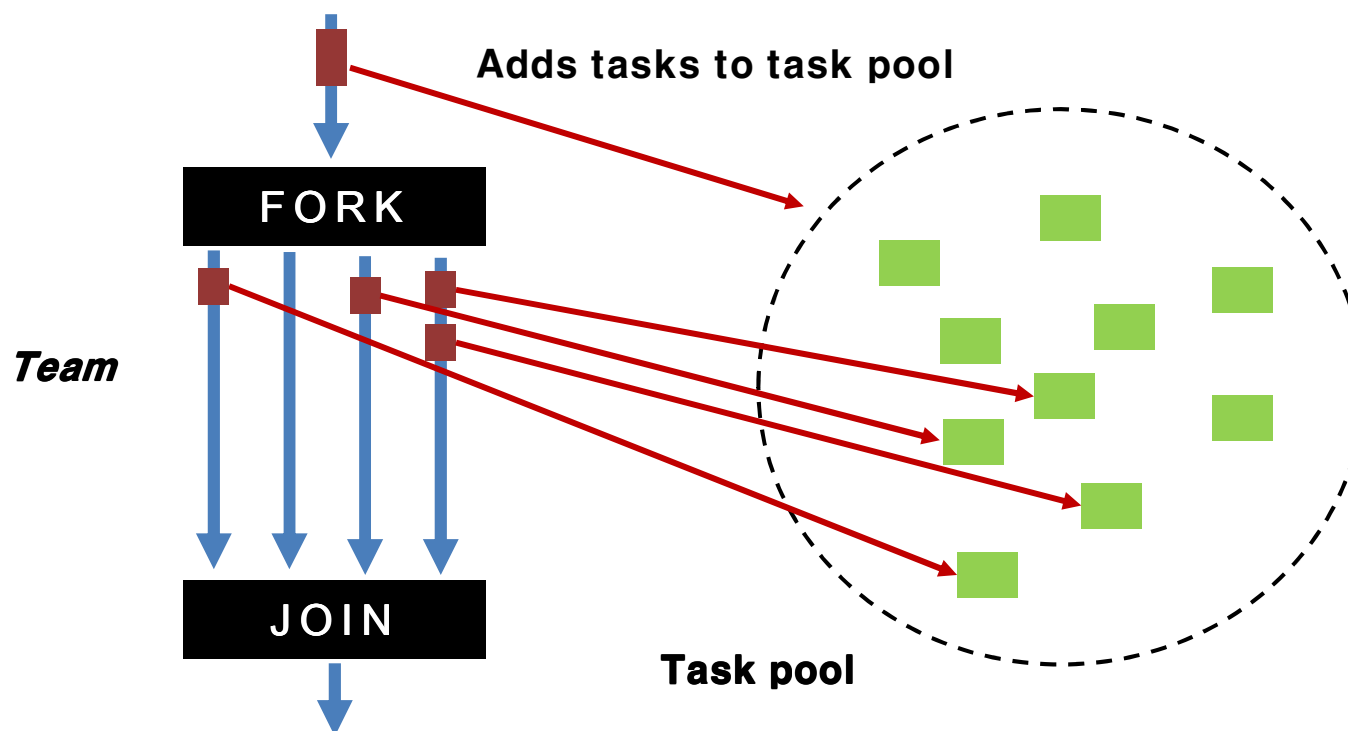


Task (2/2)



➤ TASK Construct

- New construct with OpenMP 3.0
- The TASK construct defines an explicit task, which may be executed by the encountering thread or deferred for execution by any other thread
- The data environment of the task is determined by the data sharing attribute clauses





Task : taskwait



Fortran	C
<pre> PROGRAM taskwait IMPLICIT NONE INTEGER omp_get_thread_num !\$omp parallel num_threads(32) !\$OMP SINGLE PRINT *, 'A tid =', omp_get_thread_num() !\$OMP TASK PRINT *, 'B tid =', omp_get_thread_num() !\$omp end TASK !\$OMP TASK PRINT *, 'C tid =', omp_get_thread_num() !\$omp end TASK !\$OMP TASKWAIT PRINT *, 'D tid =', omp_get_thread_num() !\$omp end SINGLE !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { #pragma omp parallel num_threads(32) { #pragma omp single { printf("A tid=%d\n", omp_get_thread_num()); } #pragma omp task { printf("B tid=%d\n", omp_get_thread_num()); } #pragma omp task { printf("C tid=%d\n", omp_get_thread_num()); } #pragma omp taskwait printf("D tid=%d\n", omp_get_thread_num()); } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o taskwait.x taskwait.f90 \$./taskwait.x </pre>	<pre> \$ gcc -fopenmp -o taskwait.x taskwait.c \$./taskwait.x </pre>



Task : Data Scoping (1/2)



Fortran	C
<pre>PROGRAM task_data_scope IMPLICIT NONE INTEGER :: a, b, c, d, e !\$omp parallel private(b,d,e) !\$OMP TASK private(e) a, b, c, d, e : private? shared? !\$omp end TASK !\$omp end parallel END</pre>	<pre>int foo() { int a, b, c,d,e; #pragma omp parallel private(b,d,e) { #pragma omp task private(e) { a, b, c, d, e : private? shared? } } }</pre>
<pre>PROGRAM task USE OMP_LIB or include "omp_lib.h" IMPLICIT NONE INTEGER :: a, b, c, d, e !\$omp parallel private(b,d,e) !\$OMP TASK private(e) a : shared b : firstprivate c : shared d : firstprivate e : private !\$omp end TASK !\$omp end parallel END</pre>	<pre>int foo() { int a, b, c,d,e; #pragma omp parallel private(b,d,e) { #pragma omp task { a : shared b : firstprivate c : shared d : firstprivate e : private } } }</pre>



Task : Data Scoping (2/2)



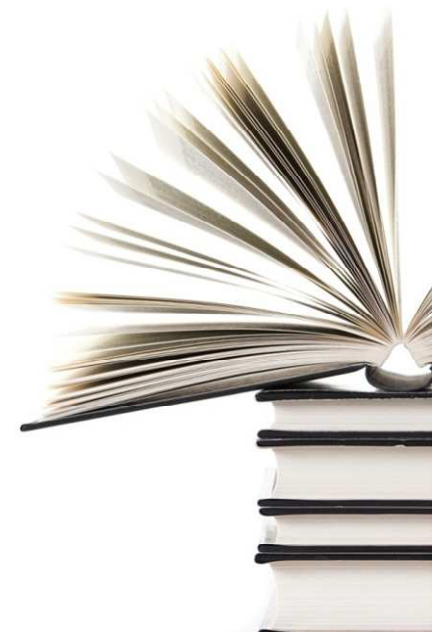
Fortran	C
<pre> PROGRAM task_data_scope IMPLICIT NONE INTEGER :: a=1, b=2, c=3, d=4, e=5 INTEGER tid, omp_get_thread_num CALL omp_set_num_threads(4) !\$omp parallel private(b,d,e,tid) tid = omp_get_thread_num() PRINT 10, 'tid=',tid, ' a=',a, ' b=',b, ' c=',c, ' d=',d, ' e=',e !\$omp single a=2; b=3; c=4; d=5;e=6 !\$omp end single !\$omp task private(e) PRINT 10, 'task tid=',omp_get_thread_num(), & & ' a=',a, ' b=',b, ' c=',c, ' d=',d, ' e=',e !\$omp end task !\$omp end parallel 10 FORMAT(A,I4,A,I4,A,I4,A,I4,A,I4,A,I4) END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int a=1, b=2, c=3, d=4, e=5, tid; omp_set_num_threads(4); #pragma omp parallel private(b,d,e, tid) { tid = omp_get_thread_num(); printf("tid=%d a=%d b=%d c=%d d=%d e=%d\n", tid, a, b, c, d, e); #pragma omp single { a=2, b=3, c=4, d=5, e=6; } #pragma omp task private(e) { printf("task tid=%d a=%d b=%d c=%d d=%d e=%d\n", omp_get_thread_num(), a, b, c, d, e); } } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o task_data_scope.x task_data_scope.f90 \$./task_data_scope.x </pre>	<pre> \$ gcc -fopenmp -o task_data_scope.x task_data_scope.c\$./task_data_scope.x </pre>

Break!!



Schedule

1. Schedule





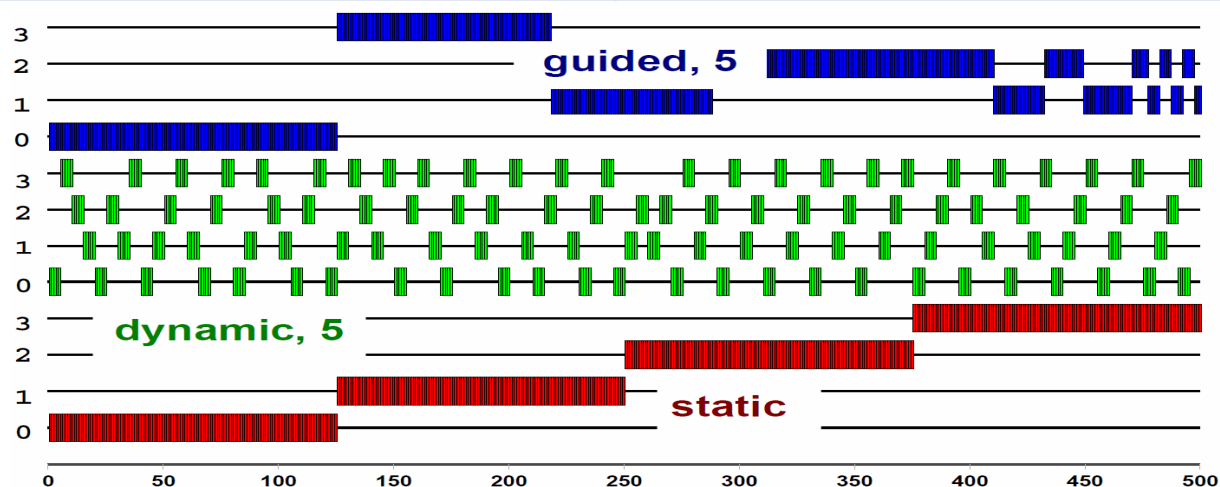
SCHEDULE



➤ Scheduling clauses

- Specifies **how iterations of the for loop are divided among the threads of the team.**
- Useful if the work sharing construct is a do-loop or for-loop. The iteration in the work sharing construct are assigned to threads according to the scheduling method defined by this clause.
- Static [, chunk]
 - Each thread is assigned a **fixed number of chunks** to work on
 - Chunks are assigned to the threads in Round-Robin fashion
- Dynamic [, chunk]
 - The assignment of iterations to threads is **determined at runtime**
- Guided [, chunk]
 - a variant of dynamic scheduling.
 - the first chunk of iterations is of some implementation-dependent size, and **the size of each successive chunk is a fixed fraction of the preceding chunk** until a minimum size of chunk_size is reached.
- runtime
 - allows the scheduling to be determined at runtime. The chunk_size PARAMETER must not appear.
 - The type is chosen at runtime based on the value of the environment variable OMP_SCHEDULE.

Fortran	C
<pre> PROGRAM static IMPLICIT NONE INTEGER :: a(0:499), I !\$omp parallel DO schedule(static) num_threads(4) DO i=0, 499 a(i) = i END DO END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int i, a[500]; #pragma omp parallel for schedule(static) num_threads(4) for(i=0; i<500; i++) a[i] = i; return 0; } </pre>
<pre> \$ gfortran -fopenmp -o static.x static.f90 \$ time ./static.x </pre>	<pre> \$ gcc -fopenmp -o static.x static.c \$ time ./static.x </pre>





SCHEDULE



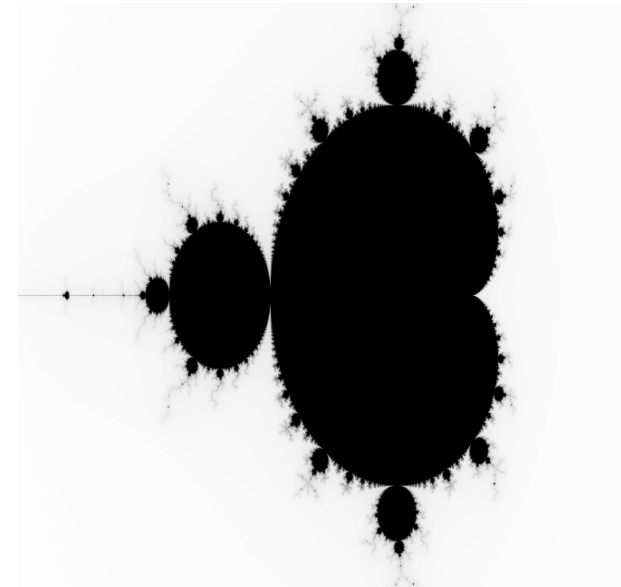
➤ Mandelbrot

- Mandelbrot is an image computing and display computation
- Pixels of an image are stored in a 2D array
- Each pixel is computed by iterating the COMPLEX function

$$Z_{k+1} = Z_k^2 + C, \quad Z_k = a_k + b_k i, \quad C = C_{real} + C_{imag} i$$

$$\begin{aligned} Z_{k+1} &= (a_k + b_k i)^2 + (C_{real} + C_{imag} i) \\ &= (a_k^2 - b_k^2 + C_{real}) + (2a_k b_k + C_{imag}) i \end{aligned}$$

- The magnitude of z is given by $Z_{length} = \sqrt{a^2 + b^2}$





SCHEDULE (Exercise)



C (Serial)

```
#include <stdio.h>

#define X_RESN 4000 /* x resolution */
#define Y_RESN 4000 /* y resolution */
#define X_MIN -2.0
#define X_MAX 2.0
#define Y_MIN -2.0
#define Y_MAX 2.0

typedef struct COMPLEXtype {
    float REAL, imag;
} Compl;

int main ( int argc, char* argv[])
{
    int i, j, k, maxIterations = 1000;
    Compl z, c;
    float lengthsq, temp;
    int res[X_RESN][Y_RESN];

    for (i=0; i < X_RESN; i++) {
        for (j=0; j < Y_RESN; j++) {
            z.REAL = z.imag = 0.0;
            c.REAL = X_MIN + j * (X_MAX - X_MIN) / X_RESN;
            c.imag = Y_MAX - i * (Y_MAX - Y_MIN) / Y_RESN;
            k = 0;

            do {
                temp = z.REAL*z.REAL - z.imag*z.imag + c.REAL;
                z.imag = 2.0*z.REAL*z.imag + c.imag;
                z.REAL = temp;
                lengthsq = z.REAL*z.REAL+z.imag*z.imag;
                k++;
            } while (lengthsq < 4.0 && k < maxIterations);

            if (k >= maxIterations) res[i][j] = 0;
            else res[i][j] = 1;
        }
    }
    return 0;
}
```

```
$ gcc -fopenmp -o schedule.x schedule.c
$ ulimit -s 512000
$ time ./schedule.x
```



SCHEDULE (Exercise)



Fortran (Serial)

```
PROGRAM mandel_serial
IMPLICIT NONE

INTEGER, PARAMETER :: X_RESN=4000, Y_RESN=4000
REAL, PARAMETER :: X_MIN=-2.0, X_MAX=2.0, &
                  Y_MIN=-2.0, Y_MAX=2.0

COMPLEX :: z, c
INTEGER :: i, j, k, maxIterations=1000
REAL :: lengthsq, temp
INTEGER, dimension(0:X_RESN-1, 0:Y_RESN-1) :: res

DO j=0, Y_RESN-1
  DO i=0, X_RESN-1
    z = (0.0, 0.0)
    c = cmplx( X_MIN+REAL(j) * (X_MAX-X_MIN) &
              / REAL(X_RESN), &
              Y_MAX - REAL(i) * (Y_MAX - Y_MIN) &
              / REAL(Y_RESN) )

    k=0
```

```
    loop: DO
      temp = REAL(z) * REAL(z) - AIMAG(z) * AIMAG(z) &
            + REAL(c)
      z=cmplx( temp, 2.0*REAL(z)*AIMAG(z)+AIMAG(c) )
      lengthsq = REAL(z)*REAL(z)+AIMAG(z)*AIMAG(z)
      k=k+1
      IF (lengthsq >= 4.0 .or. k >= maxIterations) exit loop
    END DO loop

    IF ( k >= maxIterations ) THEN
      res(i, j) = 0
    ELSE
      res(i, j) = 1
    END IF

  END DO
END DO

END
```

```
$ gfortran -fopenmp -o schedule.x schedule.f90
$ ulimit -s 512000
$ time ./schedule.x
```



SCHEDULE (Solution)



C (Parallel)

```
#include <stdio.h>
#include <omp.h>

#define X_RESN 4000 /* x resolution */
#define Y_RESN 4000 /* y resolution */
#define X_MIN -2.0
#define X_MAX 2.0
#define Y_MIN -2.0
#define Y_MAX 2.0

typedef struct COMPLEXtype {
    float REAL, imag;
} Compl;

int main ( int argc, char* argv[])
{
    int i, j, k, maxIterations = 1000;
    Compl z, c;
    float lengthsq, temp;
    int res[X_RESN][Y_RESN];

#pragma omp parallel for shared(res, maxIterations)
    private(j,z,c,k,temp,lengthsq)
    for (i=0; i < X_RESN; i++) {
        for (j=0; j < Y_RESN; j++) {
            z.REAL = z.imag = 0.0;
            c.REAL = X_MIN + j * (X_MAX - X_MIN)/X_RESN;
            c.imag = Y_MAX - i * (Y_MAX - Y_MIN)/Y_RESN;
            k = 0;

            do {
                temp = z.REAL*z.REAL - z.imag*z.imag + c.REAL;
                z.imag = 2.0*z.REAL*z.imag + c.imag;
                z.REAL = temp;
                lengthsq = z.REAL*z.REAL+z.imag*z.imag;
                k++;
            } while (lengthsq < 4.0 && k < maxIterations);

            if (k >= maxIterations) res[i][j] = 0;
            else res[i][j] = 1;
        }
    }
}
```

```
$ gcc -fopenmp -o schedule.x schedule.c
$ export OMP_NUM_THREADS=8
$ time ./schedule.x
```



SCHEDULE (Solution)



Fortran (Parallel)

```
PROGRAM solution
IMPLICIT NONE

INTEGER, PARAMETER :: X_RESN=4000, Y_RESN=4000
REAL, PARAMETER :: X_MIN=-2.0, X_MAX=2.0,
                  Y_MIN=-2.0, Y_MAX=2.0

COMPLEX :: z, c
INTEGER :: i, j, k, maxIterations=1000
REAL :: lengthsq, temp
INTEGER, dimension(0:X_RESN-1, 0:Y_RESN-1) :: res

!$omp parallel DO shared(res, maxIterations) private(z, c, k, temp,
lengthsq)
DO j=0, Y_RESN-1
  DO i=0, X_RESN-1
    z = (0.0, 0.0)
    c = cmplx( X_MIN + REAL(j) * (X_MAX - Y_MIN)
              / REAL(X_RESN),
              Y_MAX - REAL(i) * (Y_MAX - Y_MIN)
              / REAL(Y_RESN) )

    k=0
```

```
    loop: DO
      temp = REAL(z) * REAL(z) - AIMAG(z) * AIMAG(z)
            + REAL(c)
      z=cmplx( temp, 2.0*REAL(z)*AIMAG(z)+AIMAG(c) )
      lengthsq = REAL(z)*REAL(z)+AIMAG(z)*AIMAG(z)
      k=k+1
      IF (lengthsq >= 4.0 .or. k >= maxIterations) exit loop
    END DO loop

    IF ( k >= maxIterations ) THEN
      res(i, j) = 0
    ELSE
      res(i, j) = 1
    END IF

  END DO
ENDDO

END
```

```
$ gfortran -fopenmp -o schedule.x schedule.f90
$ export OMP_NUM_THREADS=8
$ time ./schedule.x
```



SCHEDULE (Solution Cont.)



C (parallel with dynamic schedule)

```
#include <stdio.h>
#include <omp.h>

#define X_RESN 4000 /* x resolution */
#define Y_RESN 4000 /* y resolution */
#define X_MIN -2.0
#define X_MAX 2.0
#define Y_MIN -2.0
#define Y_MAX 2.0

typedef struct COMPLEXtype {
    float REAL, imag;
} Compl;

int main ( int argc, char* argv[])
{
    int i, j, k, maxIterations = 1000;
    Compl z, c;
    float lengthsq, temp;
    int res[X_RESN][Y_RESN];

    #pragma omp parallel for shared(res, maxIterations)
    private(j,z,c,k,temp,lengthsq) schedule(dynamic, 5)
    for(i=0; i < X_RESN; i++) {
        for(j=0; j < Y_RESN; j++) {
            z.REAL = z.imag = 0.0;
            c.REAL = X_MIN + j * (X_MAX - X_MIN)/X_RESN;
            c.imag = Y_MAX - i * (Y_MAX - Y_MIN)/Y_RESN;
            k = 0;

            do {
                temp = z.REAL * z.REAL - z.imag * z.imag + c.REAL;
                z.imag = 2.0 * z.REAL * z.imag + c.imag;
                z.REAL = temp;
                lengthsq = z.REAL * z.REAL + z.imag * z.imag;
                k++;
            } while (lengthsq < 4.0 && k < maxIterations);

            IF (k >= maxIterations) res[i][j] = 0;
            ELSE res[i][j] = 1;
        }
    }
}
```

```
$ gcc -fopenmp -o schedule.x schedule.c
$ export OMP_NUM_THREADS=8
$ time ./schedule.x
```



SCHEDULE (Exercise)



Fortran (Parallel)

```
PROGRAM ex
USE OMP_LIB or include "omp_lib.h"
IMPLICIT NONE

INTEGER, PARAMETER :: X_RESN=4000, Y_RESN=4000
REAL, PARAMETER :: X_MIN=-2.0, X_MAX=2.0, Y_MIN=-2.0, Y_MAX=2.0

COMPLEX :: z, c
INTEGER :: i, j, k, maxIterations=1000
REAL :: lengthsq, temp
INTEGER, dimension(0:X_RESN-1, 0:Y_RESN-1) :: res

!$omp parallel DO shared(res, maxIterations) private(z, c, k, temp,
lengthsq) schedule(dynamic, 5)
DO j=0, Y_RESN-1
  DO i=0, X_RESN-1
    z = (0.0, 0.0)
    c = cmplx( X_MIN+REAL(j)*(X_MAX-X_MIN) /
REAL(X_RESN), Y_MAX-REAL(i) * (Y_MAX-Y_MIN) /
REAL(Y_RESN) )
```

```
    k=0
    loop : DO
      temp = REAL(z)*REAL(z)-AIMAG(z)*AIMAG(z) +
REAL(c)
      z=cmplx( temp, 2.0*REAL(z)*AIMAG(z)+AIMAG(c) )
      lengthsq = REAL(z)*REAL(z)+AIMAG(z)*AIMAG(z)
      k=k+1
      if (lengthsq >= 4.0 && k >= maxIterations) THEN
        exit loop
      END DO loop

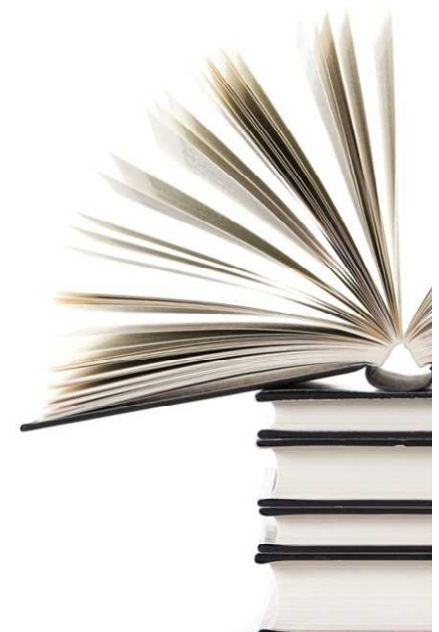
      if ( k >= maxIterations ) THEN
        res(i, j) = 0
      else
        res(i, j) = 1
      END IF

    END DO
  ENDDO
END
```

```
$ gfortran -fopenmp -o schedule.x schedule.f90
$ export OMP_NUM_THREADS=8
$ time ./schedule.x
```

OpenMP Performance Issue

- 1. Nested Parallel (Collapse)**
- 2. Flush**
- 3. False Sharing**
- 4. DepENDency**





Collapse (1/4)



Fortran	C
<pre>PROGRAM collapse USE OMP_LIB or include "omp_lib.h" IMPLICIT NONE INTEGER, PARAMETER :: N=10000 INTEGER :: a(0:N-1, 0:N-1), i, j CALL omp_set_nested(1) CALL omp_set_num_threads(4) !\$omp parallel do private(i, j) DO i=0, N-1 !\$omp parallel do DO j=0, N-1 a(i, j) = a(i, j) * 2 END DO END DO END</pre>	<pre>#include <stdio.h> #include <omp.h> #define N 10000 int main() { int a[N][N], i, j; omp_set_nested(1); omp_set_num_threads(4); #pragma omp parallel for private(i,j) for(i=0; i<N; i++) { #pragma omp parallel for for(j=0; j<N; j++) a[i][j] = a[i][j] * 2; } return 0; }</pre> Better performance?



Collapse (2/4)



Fortran	C
<pre>PROGRAM collapse2 USE OMP_LIB or include "omp_lib.h" IMPLICIT NONE INTEGER, PARAMETER :: N=10000 INTEGER :: a(0:N-1, 0:N-1), i, j CALL omp_set_nested(1) CALL omp_set_num_threads(4) !\$omp parallel private(i, j) !\$OMP DO DO i=0, N-1 !\$OMP DO DO j=0, N-1 a(i, j) = a(i, j) * 2 END DO END DO END</pre>	<pre>#include <stdio.h> #include <omp.h> #define N 10000 int main() { int a[N][N], i, j; omp_set_nested(1); omp_set_num_threads(4); #pragma omp parallel private(i,j) { #pragma omp for for(i=0; i<N; i++) { #pragma omp for for(j=0; j<N; j++) a[i][j] = a[i][j] * 2; } } return 0; }</pre>

Possible ???



Collapse (3/4)



Fortran	C
<pre>PROGRAM collapse3 IMPLICIT NONE INTEGER, PARAMETER :: N=10000 INTEGER :: a(0:N-1, 0:N-1), i CALL omp_set_num_threads(4) !\$omp parallel DO DO i=0, N*N-1 a(i/N, MOD(i, N)) = a(i/N, MOD(i, N)) * 2 END DO END</pre>	<pre>#include <stdio.h> #include <omp.h> #define N 10000 int main() { static int a[N][N], i, j; omp_set_num_threads(4); #pragma omp parallel for for(i=0; i<N*N; i++) a[i/N][i%N] = a[i/N][j%N] * 2; return 0; }</pre>
<pre>\$ gfortran -fopenmp -o collapse.x collapse.f90 \$ ulimit -s 512000 \$ time ./collapse.x</pre>	<pre>\$ gcc -fopenmp -o collapse.x collapse.c \$ time ./collapse.x</pre>



Collapse (4/4)



Fortran	C
<pre>PROGRAM collapse4 IMPLICIT NONE INTEGER, PARAMETER :: N=9999 INTEGER :: a(0:N, 0:N), i, j CALL omp_set_num_threads(4) !\$omp parallel do private(i, j) collapse(2) DO j=0, N DO i=0, N a(i, j) = a(i, j) * 2 END DO END DO !\$omp end parallel do END</pre>	<pre>#include <stdio.h> #include <omp.h> #define N 10000 int main() { int a[N][N], i, j; omp_set_num_threads(4); #pragma omp parallel for private(i,j) collapse(2) for(i=0; i<N; i++) for(j=0; j<N; j++) a[i][j] = a[i][j] * 2; return 0; }</pre>
<pre>\$ gfortran -fopenmp -o collapse4.x collapse4.f90 \$ ulimit -s 512000 \$ time ./collapse4.x</pre>	<pre>\$ gcc -fopenmp -o collapse4.x collapse4.c \$ time ./collapse4.x</pre>



Flush (1/3)



Fortran	C
<pre> PROGRAM flush1 IMPLICIT NONE INTEGER :: x=0, tid, omp_get_thread_num CALL omp_set_num_threads(4) !\$omp parallel private(tid) tid = omp_get_thread_num() IF (tid == 0) THEN CALL sleep(3) x = 1 CALL sleep(3) END IF DO WHILE (x == 0) END DO PRINT *, "x =", x, "in", tid, "-th thread" !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int x=0, tid; omp_set_num_threads(4); #pragma omp parallel private(tid) { tid = omp_get_thread_num(); if (tid == 0) { sleep(3); x = 1; sleep(3); } while(x == 0) { } printf("x=%d in %d-th thread\n", x, tid); } return 0; } </pre>
<pre> \$ gfortran -fopenmp -o ok.x flush.f90 \$./ok.x \$ gfortran -O3 -fopenmp -o no.x flush.f90 \$./no.x </pre>	<pre> \$ gcc -fopenmp -o ok.x flush.c \$./ok.x \$ gcc -O3 -fopenmp -o no.x flush.c \$./no.x </pre>



Flush (2/3)



➤ FLUSH Directive

- Acts as a **memory barrier/fence**
- The compiler and hardware do not reorder your reads and WRITES
- cf. volatile, WRITE-through, WRITE-back

```
while( x == 0 ) {  
}  
x = x + 1;
```

Pseudo code

Without optimization option

```
L1:  
  mov eax, 0x7c385400  
  cmp eax, 0  
  je L1  
  mov eax, 0x7c385400  
  inc eax  
  mov 0x7c385400, eax
```

With optimization option (-O3)

```
  mov eax, 0x7c385400  
L1:  
  cmp eax, 0  
  je L1  
  inc eax  
  mov 0x7c385400, eax
```



Flush (3/3)



Fortran	C
<pre> PROGRAM flush2 IMPLICIT NONE INTEGER :: x=0, tid CALL omp_set_num_threads(4) !\$omp parallel private(tid) tid = omp_get_thread_num() IF (tid == 0) THEN CALL sleep(3) x = 1 CALL sleep(3) END IF DO WHILE (x == 0) !\$OMP FLUSH(x) END DO PRINT *, "x =", x, "in", tid, "-th thread" !\$omp end parallel END </pre>	<pre> #include <stdio.h> #include <omp.h> int main() { int x=0, tid; omp_set_num_threads(4); #pragma omp parallel private(tid) { tid = omp_get_thread_num(); if (tid == 0) { sleep(3); x = 1; sleep(3); } while (x == 0) { #pragma omp flush(x) } printf("x=%d in %d-th thread\n", x, tid); } return 0; } </pre>
<pre> \$ gfortran -O3 -fopenmp -o flush.x flush.c \$./flush.x </pre>	<pre> \$ gcc -O3 -fopenmp -o flush.x flush.c \$./flush.x </pre>



False Sharing (1/4)



Fortran	C
<pre> PROGRAM false_sharing IMPLICIT NONE INTEGER, PARAMETER :: N=1000000000 INTEGER(8) :: total_sum=0, a(0:3) INTEGER i, tid, omp_get_thread_num a=0 CALL omp_set_num_threads(4) !\$omp parallel private(tid) tid = omp_get_thread_num() !\$OMP DO DO i=1, N a(tid) = a(tid) + i END DO !\$OMP ATOMIC total_sum = total_sum + a(tid) !\$omp end parallel PRINT *, "sum =", total_sum END </pre>	<pre> #include <stdio.h> #include <omp.h> #define N 1000000000 int main() { long sum=0, a[4] = { 0 }, i, tid; omp_set_num_threads(4); #pragma omp parallel private(tid) { tid = omp_get_thread_num(); #pragma omp for for(i=1; i<=N; i++) a[tid] += i; #pragma omp atomic sum += a[tid]; } printf("sum = %ld\n", sum); return 0; } </pre>
<pre> \$ gfortran -fopenmp -o false_sharing.x false_sharing.f90 \$ time ./false_sharing.x </pre>	<pre> \$ gcc -fopenmp -o false_sharing.x false_sharing.c \$ time ./false_sharing.x </pre>

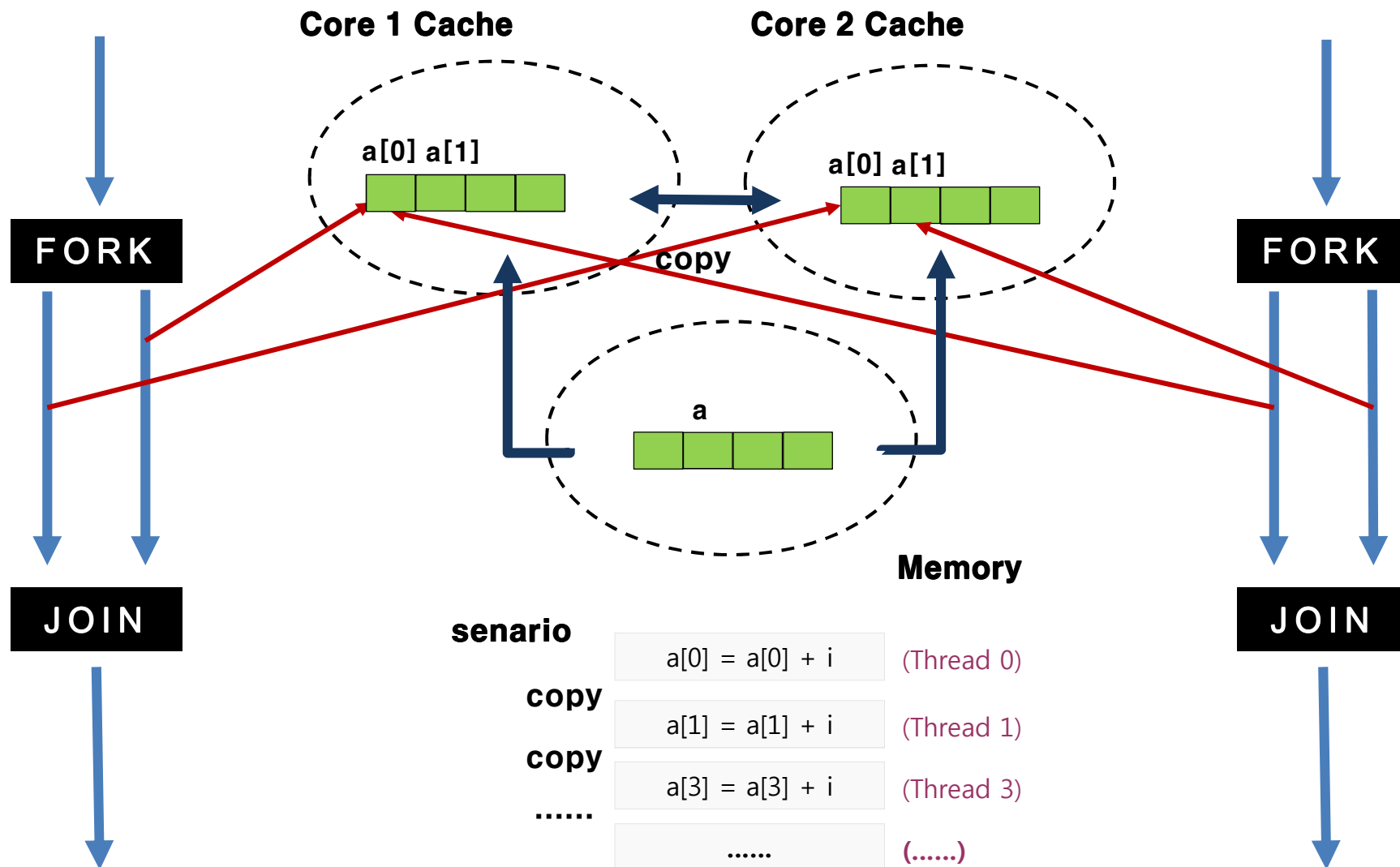


False Sharing (2/4)



True sharing

False sharing





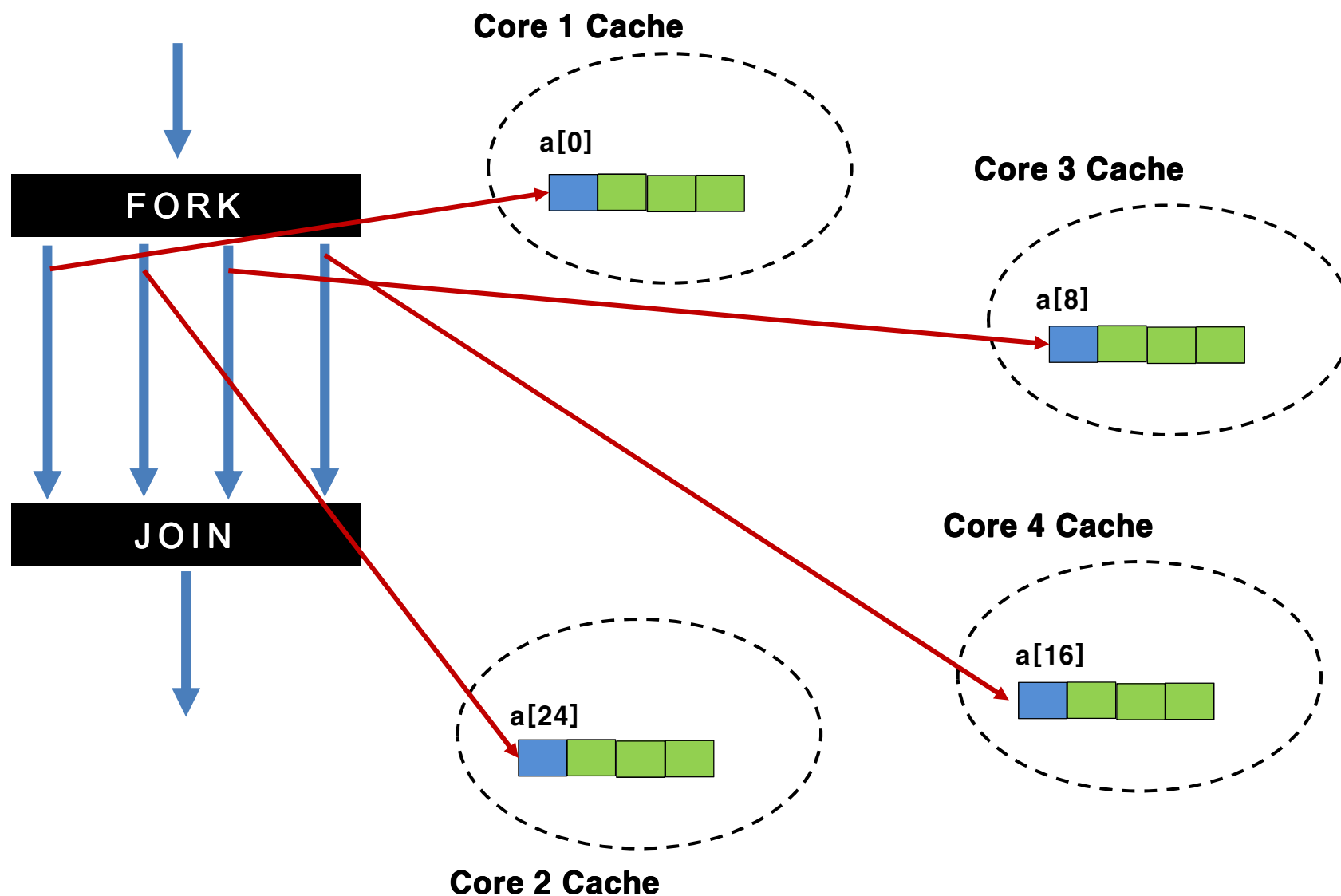
False Sharing (3/4)



Fortran	C
<pre> PROGRAM false_sharing_solved IMPLICIT NONE INTEGER, PARAMETER :: N=1000000000 INTEGER(8) :: total_sum=0, a(0:3*8) INTEGER i, tid, omp_get_thread_num a=0 CALL omp_set_num_threads(4) !\$omp parallel private(tid) tid = omp_get_thread_num() !\$OMP DO DO i=1, N a(tid*8) = a(tid*8) + i END DO !\$OMP ATOMIC total_sum = total_sum + a(tid*8) !\$omp end parallel PRINT *, "sum =", total_sum END </pre>	<pre> #include <stdio.h> #include <omp.h> #define N 1000000000 int main() { long sum=0, a[4*8] = { 0 }, i, tid; omp_set_num_threads(4); #pragma omp parallel private(tid) { tid = omp_get_thread_num(); #pragma omp for for(i=1; i<=N; i++) a[tid*8] += i; #pragma omp atomic sum += a[tid*8]; } printf("sum = %ld\n", sum); return 0; } </pre>
<pre> \$ gfortran -fopenmp -o false_sharing_sol.x false_sharing_sol.f90 \$ time ./false_sharing_sol.x </pre>	<pre> \$ gcc -fopenmp -o false_sharing_sol.x false_sharing_sol.c \$ time ./false_sharing_sol.x </pre>



False Sharing (4/4)





False Sharing (4/4)



Fortran	C
<pre> PROGRAM use_local_sum IMPLICIT NONE INTEGER, PARAMETER :: N=1000000000 INTEGER(8) :: total_sum=0, local_sum INTEGER i, tid, omp_get_thread_num CALL omp_set_num_threads(4) !\$omp parallel private(tid, local_sum) local_sum = 0 tid = omp_get_thread_num() !\$OMP DO DO i=1, N local_sum = local_sum + i END DO !\$OMP ATOMIC total_sum = total_sum + local_sum !\$omp end parallel PRINT *, "sum =", total_sum END </pre>	<pre> #include <stdio.h> #include <omp.h> #define N 1000000000 int main() { long sum=0, local_sum, i, tid; omp_set_num_threads(4); #pragma omp parallel private(tid, local_sum) { local_sum = 0; tid = omp_get_thread_num(); #pragma omp for for(i=1; i<=N; i++) local_sum += i; #pragma omp atomic sum += local_sum; } printf("sum = %ld\n", sum); return 0; } </pre>
<pre> \$ gfortran -fopenmp -o use_local_sum.x use_local_sum.f90 \$ time ./use_local_sum.x </pre>	<pre> \$ gcc -fopenmp -o use_local_sum.x use_local_sum.c \$ time ./use_local_sum.x </pre>



Data Dependency (1/2)



Fortran	C
<pre>DO time=0, max_time-1 DO j=1, n-2 DO i=1, n-2 h(i, j) = 0.25 * (h(i-1, j) + h(i+1, j) + h(i, j-1) + h(i, j+1)) END DO END DO END DO</pre>	<pre>for (time=0; time < max_time; time++) { for (i=1; i<n-1; i++) for (j=1; j<n-1; j++) h[i][j] = 0.25 * (h[i-1][j] + h[i+1][j] + h[i][j-1] + h[i][j+1]); }</pre>
<pre>DO time=0, max_time-1 !\$omp parallel DO DO j=1, n-2 DO i=1, n-2 newh(i, j) = 0.25 * (h(i-1, j) + h(i+1, j) + h(i, j-1) + h(i, j+1)) END DO END DO !\$omp parallel DO DO j=1, n-2 DO i=1, n-2 h(i, j) = newh(i, j) END DO END DO END DO</pre>	<pre>for(time=0; time < max_time; time++) { #pragma omp parallel for private(j) for(i=1; i<n-1; i++) for(j=1; j<n-1; j++) newh[i][j] = 0.25 * (h[i-1][j] + h[i+1][j] + h[i][j-1] + h[i][j+1]); #pragma omp parallel for private(j) for(i=1; i<n-1; i++) for(j=1; j<n-1; j++) h[i][j] = newh[i][j]; }</pre>

➤ Heat Distribution Problem

$$h_{i,j} = \frac{h_{i-1,j} + h_{i+1,j} + h_{i,j-1} + h_{i,j+1}}{4}$$



Data Dependency (2/2)



Fortran	C
<pre>PROGRAM fibonacci IMPLICIT NONE INTEGER, PARAMETER :: N=10 INTEGER :: i DO i=0, N PRINT *, "fibonacci F(", i, ") =", fibon(i) END DO CONTAINS recursive INTEGER function fibon(n) RESULT(fib) INTEGER :: n IF (n < 2) THEN fib = n ELSE fib = fibon(n-1) + fibon(n-2) END IF END function END PROGRAM</pre>	<pre>#include <stdio.h> #define N 10 int fibon(int n) { if (n < 2) return n; return (fibon(n-1) + fibon(n-2)); } int main() { int i; for (i=0; i<=N; i++) printf("fibonacci F(%d) = %d\n", i, fibon(i)); return 0; }</pre>
<pre>\$ gfortran -fopenmp -o fibonacci.x fibonacci.f90 \$./fibonacci.x</pre>	<pre>\$ gcc -fopenmp -o fibonacci.x fibonacci.c \$./fibonacci.x</pre>

➤ Fibonacci

– $F(n) = F(n-1) + F(n-2)$, $F(0) = 0$, $F(1) = 1$, $n = 2, 3, 4, \dots$



Data Dependency (2/2)



Fortran	C
<pre>PROGRAM fibonacci IMPLICIT NONE INTEGER, PARAMETER :: N=10 INTEGER :: i INTEGER, dimension(0:N) :: fibon fibon(0) = 0 fibon(1) = 1 DO i=2, N fibon(i) = fibon(i-1) + fibon(i-2) END DO DO i=0, N PRINT *, "fibonacci F(", i, ") =", fibon(i) END DO END</pre>	<pre>#include <stdio.h> #define N 10 int main() { int i, fibon[N+1]; fibon[0] = 0; fibon[1] = 1; for(i=2; i<=N; i++) { fibon[i] = fibon[i-1] + fibon[i-2]; } for(i=0; i<=N; i++) printf("fibonacci F(%d) = %d\n", i, fibon[i]); return 0; }</pre>
<pre>\$ gfortran -fopenmp -o fibonacci2.x fibonacci2.f90 \$./fibonacci2.x</pre>	<pre>\$ gcc -fopenmp -o fibonacci2.x fibonacci.c \$./fibonacci2.x</pre>

➤ Fibonacci

– $F(n) = F(n-1) + F(n-2)$, $F(0) = 0$, $F(1) = 1$, $n = 2, 3, 4, \dots$



Data Dependency (2/2)



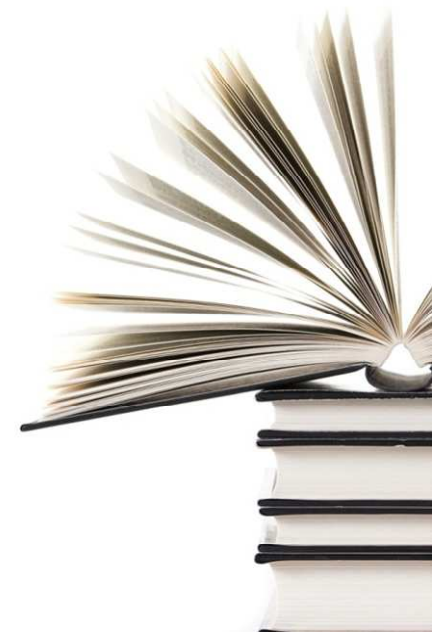
Fortran	C
<pre> PROGRAM fibonacci IMPLICIT NONE INTEGER, PARAMETER :: N=10 INTEGER i, fibon(0:N) DOUBLE PRECISION :: alpha, beta, c alpha=0.5*(1.0+sqrt(REAL(5))) beta=0.5*(1.0-sqrt(REAL(5))) c=1/sqrt(REAL(5)) !\$omp parallel DO num_threads(2) DO i=0, N fibon(i) = c * (alpha**i-beta**i) END DO DO i=0, N PRINT *, "fibonacci F(", i, ") =", fibon(i) END DO END </pre>	<pre> #include <stdio.h> #include <math.h> #include <omp.h> #define N 10 int main() { int i, fibon[N+1]; double alpha = 0.5 * (1.0+sqrt(5)); double beta = 0.5 * (1.0-sqrt(5)); double c = 1 / sqrt(5); #pragma omp parallel for num_threads(2) for(i=0; i<=10; i++) fibon[i] = c * (pow(alpha,i)-pow(beta,i)); for(i=0; i<=N; i++) printf("fibonacci F(%d) = %d\n", i, fibon[i]); return 0; } </pre>
<pre> \$ gfortran -fopenmp -o fibonacci3.x fibonacci3.f90 \$./fibonacci3.x </pre>	<pre> \$ gcc -fopenmp -o fibonacci3.x fibonacci3.c -lm \$./fibonacci3.x </pre>

➤ Fibonacci

$$F(n) = F(n-1) + F(n-2), F(0) = 0, F(1) = 1, n = 2, 3, \dots \quad F(n) = \frac{1}{\sqrt{5}} \left\{ \left(\frac{1+\sqrt{5}}{2} \right)^n - \left(\frac{1-\sqrt{5}}{2} \right)^n \right\}$$

Hands-on

- 1. Matrix Multiplication**
- 2. LU Decomposition (Optional)**
- 3. Fibonacci (Optional)**





Ex1. Matrix Multiplication



```
// KISTI educational Matrix
// Multiplication problem
// Copyright (c) 2012 KISTI
// Supercomputing Center

#include <stdio.h>
#define N 10

int main()
{
    int i,j,k;
    int a[N][N], b[N][N], c[N][N];

    for(i=0; i<N; i++) {
        for(j=0; j<i; j++) {
            a[i][j] = b[i][j] = c[i][j] = 0;
        }
        for(j=i; j<N; j++) {
            a[i][j] = i+j+1;
            b[i][j] = i+j+2;
            c[i][j] = 0;
        }
    }

    for(i=0; i<N; i++)
        for(j=0; j<N; j++)
            for(k=0; k<N; k++)
                c[i][j] += a[i][k] * b[k][j];
```

```
printf("matrix a\n");
for(i=0; i<N; i++) {
    for(j=0; j<N; j++)
        printf("%4d ", a[i][j]);
    printf("\n");
}

printf("matrix b\n");
for(i=0; i<N; i++) {
    for(j=0; j<N; j++)
        printf("%4d ", b[i][j]);
    printf("\n");
}

printf("matrix c\n");
for(i=0; i<N; i++) {
    for(j=0; j<N; j++)
        printf("%4d ", c[i][j]);
    printf("\n");
}
```

a

1	2	3	4	5	6	7	8	9	10
0	3	4	5	6	7	8	9	10	11
0	0	5	6	7	8	9	10	11	12
0	0	0	7	8	9	10	11	12	13
0	0	0	0	9	10	11	12	13	14
0	0	0	0	0	11	12	13	14	15
0	0	0	0	0	0	13	14	15	16
0	0	0	0	0	0	0	15	16	17
0	0	0	0	0	0	0	0	17	18
0	0	0	0	0	0	0	0	0	19

b

2	3	4	5	6	7	8	9	10	11
0	4	5	6	7	8	9	10	11	12
0	0	6	7	8	9	10	11	12	13
0	0	0	8	9	10	11	12	13	14
0	0	0	0	10	11	12	13	14	15
0	0	0	0	0	12	13	14	15	16
0	0	0	0	0	0	14	15	16	17
0	0	0	0	0	0	0	16	17	18
0	0	0	0	0	0	0	0	18	19
0	0	0	0	0	0	0	0	0	20

c

2	11	32	70	130	217	336	492	690	935
0	12	39	86	158	260	397	574	796	1068
0	0	30	83	164	278	430	625	868	1164
0	0	0	56	143	266	430	640	901	1218
0	0	0	0	90	219	392	614	890	1225
0	0	0	0	0	132	311	542	830	1180
0	0	0	0	0	0	182	419	716	1078
0	0	0	0	0	0	0	240	543	914
0	0	0	0	0	0	0	0	306	683
0	0	0	0	0	0	0	0	0	380



Ex1. Matrix Multiplication



```
// KISTI educational Matrix
// Multiplication problem
// Copyright (c) 2012 KISTI
// Supercomputing Center
```

```
PROGRAM ex1
  IMPLICIT NONE
  INTEGER, PARAMETER :: N=9
  INTEGER :: i, j, k, a(0:N,0:N), b(0:N,0:N),
    c(0:N,0:N)
  a = 0
  b = 0
  c = 0
  DO j=0, N
    DO i=0, j
      a(i, j) = i + j + 1
      b(i, j) = i + j + 2
    END DO
  END DO

  DO j=0, N
    DO i=0, N
      DO k=0, N
        c(i, j) = c(i, j) + a(i, k) * b(k, j)
      END DO
    END DO
  END DO
```

```
PRINT *, "matrix a"
DO i=0, N
  WRITE(*, 100) (a(i, j), j=0, N)
END DO

PRINT *, "matrix b"
DO i=0, N
  WRITE(*, 100) (b(i, j), j=0, N)
END DO

PRINT *, "matrix c"
DO i=0, N
  WRITE(*, 100) (c(i, j), j=0, N)
END DO

100 FORMAT(10(i4))

END
```

a

1	2	3	4	5	6	7	8	9	10
0	3	4	5	6	7	8	9	10	11
0	0	5	6	7	8	9	10	11	12
0	0	0	7	8	9	10	11	12	13
0	0	0	0	9	10	11	12	13	14
0	0	0	0	0	11	12	13	14	15
0	0	0	0	0	0	13	14	15	16
0	0	0	0	0	0	0	15	16	17
0	0	0	0	0	0	0	0	17	18
0	0	0	0	0	0	0	0	0	19

b

2	3	4	5	6	7	8	9	10	11
0	4	5	6	7	8	9	10	11	12
0	0	6	7	8	9	10	11	12	13
0	0	0	8	9	10	11	12	13	14
0	0	0	0	10	11	12	13	14	15
0	0	0	0	0	12	13	14	15	16
0	0	0	0	0	0	14	15	16	17
0	0	0	0	0	0	0	16	17	18
0	0	0	0	0	0	0	0	18	19
0	0	0	0	0	0	0	0	0	20

c

2	11	32	70	130	217	336	492	690	935
0	12	39	86	158	260	397	574	796	1068
0	0	30	83	164	278	430	625	868	1164
0	0	0	56	143	266	430	640	901	1218
0	0	0	0	90	219	392	614	890	1225
0	0	0	0	0	132	311	542	830	1180
0	0	0	0	0	0	182	419	716	1078
0	0	0	0	0	0	0	240	543	914
0	0	0	0	0	0	0	0	306	683
0	0	0	0	0	0	0	0	0	380



Ex1. Matrix Multiplication



```
// KISTI educational Matrix
// Multiplication problem
// Copyright (c) 2012 KISTI
// Supercomputing Center
```

```
#include <stdio.h>
```

```
#define N 10
```

```
int main()
```

```
{
```

```
    int i,j,k;
```

```
    int a[N][N], b[N][N], c[N][N];
```

```
    for(i=0; i<N; i++) {
```

```
        for(j=0; j<i; j++) {
```

```
            a[i][j] = b[i][j] = c[i][j] = 0;
```

```
        }
```

```
        for(j=i; j<N; j++) {
```

```
            a[i][j] = i+j+1;
```

```
            b[i][j] = i+j+2;
```

```
            c[i][j] = 0;
```

```
        }
```

```
    }
```

```
    for(i=0; i<N; i++)
```

```
        for(j=i; j<N; j++)
```

```
            for(k=i; k<j+1; k++)
```

```
                c[i][j] += a[i][k] * b[k][j];
```

a

1	2	3	4	5	6	7	8	9	10
0	3	4	5	6	7	8	9	10	11
0	0	5	6	7	8	9	10	11	12
0	0	0	7	8	9	10	11	12	13
0	0	0	0	9	10	11	12	13	14
0	0	0	0	0	11	12	13	14	15
0	0	0	0	0	0	13	14	15	16
0	0	0	0	0	0	0	15	16	17
0	0	0	0	0	0	0	0	17	18
0	0	0	0	0	0	0	0	0	19

b

2	3	4	5	6	7	8	9	10	11
0	4	5	6	7	8	9	10	11	12
0	0	6	7	8	9	10	11	12	13
0	0	0	8	9	10	11	12	13	14
0	0	0	0	10	11	12	13	14	15
0	0	0	0	0	12	13	14	15	16
0	0	0	0	0	0	14	15	16	17
0	0	0	0	0	0	0	16	17	18
0	0	0	0	0	0	0	0	18	19
0	0	0	0	0	0	0	0	0	20

i=4, j=4

for(k=4; k<5; k++)

c[4][4] = a[4][k] * b[k][4];

c

2	11	32	70	130	217	336	492	690	935
0	12	39	86	158	260	397	574	796	1068
0	0	30	83	164	278	430	625	868	1164
0	0	0	56	143	266	430	640	901	1218
0	0	0	0	90	219	392	614	890	1225
0	0	0	0	0	132	311	542	830	1180
0	0	0	0	0	0	182	419	716	1078
0	0	0	0	0	0	0	240	543	914
0	0	0	0	0	0	0	0	306	683
0	0	0	0	0	0	0	0	0	380



Ex1. Matrix Multiplication



```
// KISTI educational Matrix
// Multiplication problem
// Copyright (c) 2012 KISTI
// Supercomputing Center
```

```
PROGRAM ex1
  IMPLICIT NONE
  INTEGER, PARAMETER :: N=9
  INTEGER :: i, j, k, a(0:N,0:N), b(0:N,0:N),
    c(0:N,0:N)
  a = 0
  b = 0
  c = 0
  DO j=0, N
    DO i=0, j
      a(i, j) = i + j + 1
      b(i, j) = i + j + 2
    END DO
  END DO

  DO j=0, N
    DO i=0, j
      DO k=i, j
        c(i, j) = c(i, j) + a(i, k) * b(k, j)
      END DO
    END DO
  END DO
```

a

1	2	3	4	5	6	7	8	9	10
0	3	4	5	6	7	8	9	10	11
0	0	5	6	7	8	9	10	11	12
0	0	0	7	8	9	10	11	12	13
0	0	0	0	9	10	11	12	13	14
0	0	0	0	0	11	12	13	14	15
0	0	0	0	0	0	13	14	15	16
0	0	0	0	0	0	0	15	16	17
0	0	0	0	0	0	0	0	17	18
0	0	0	0	0	0	0	0	0	19

b

2	3	4	5	6	7	8	9	10	11
0	4	5	6	7	8	9	10	11	12
0	0	6	7	8	9	10	11	12	13
0	0	0	8	9	10	11	12	13	14
0	0	0	0	10	11	12	13	14	15
0	0	0	0	0	12	13	14	15	16
0	0	0	0	0	0	14	15	16	17
0	0	0	0	0	0	0	16	17	18
0	0	0	0	0	0	0	0	18	19
0	0	0	0	0	0	0	0	0	20

```
i=4, j=4
for(k=4; k<5; k++)
  c[4][4] = a[4][k] * b[k][4];
```

c

2	11	32	70	130	217	336	492	690	935
0	12	39	86	158	260	397	574	796	1068
0	0	30	83	164	278	430	625	868	1164
0	0	0	56	143	266	430	640	901	1218
0	0	0	0	90	219	392	614	890	1225
0	0	0	0	0	132	311	542	830	1180
0	0	0	0	0	0	182	419	716	1078
0	0	0	0	0	0	0	240	543	914
0	0	0	0	0	0	0	0	306	683
0	0	0	0	0	0	0	0	0	380



Ex1. Matrix Multiplication



```
// KISTI educational Matrix
// Multiplication problem
// Copyright (c) 2012 KISTI
// Supercomputing Center
```

```
#include <stdio.h>
#define N 10
```

```
int main()
{
    int i,j,k;
    int a[N][N], b[N][N], c[N][N];
```

```
    for(i=0; i<N; i++) {
        for(j=0; j<i; j++) {
            a[i][j] = b[i][j] = c[i][j] = 0;
        }
        for(j=i; j<N; j++) {
            a[i][j] = i+j+1;
            b[i][j] = i+j+2;
            c[i][j] = 0;
        }
    }
```

```
    for(i=0; i<N; i++)
        for(j=i; j<N; j++)
            for(k=i; k<j+1; k++)
                c[i][j] += a[i][k] * b[k][j];
```

a

1	2	3	4	5	6	7	8	9	10
0	3	4	5	6	7	8	9	10	11
0	0	5	6	7	8	9	10	11	12
0	0	0	7	8	9	10	11	12	13
0	0	0	0	9	10	11	12	13	14
0	0	0	0	0	11	12	13	14	15
0	0	0	0	0	0	13	14	15	16
0	0	0	0	0	0	0	15	16	17
0	0	0	0	0	0	0	0	17	18
0	0	0	0	0	0	0	0	0	19

b

2	3	4	5	6	7	8	9	10	11
0	4	5	6	7	8	9	10	11	12
0	0	6	7	8	9	10	11	12	13
0	0	0	8	9	10	11	12	13	14
0	0	0	0	10	11	12	13	14	15
0	0	0	0	0	12	13	14	15	16
0	0	0	0	0	0	14	15	16	17
0	0	0	0	0	0	0	16	17	18
0	0	0	0	0	0	0	0	18	19
0	0	0	0	0	0	0	0	0	20

i=4, j=5
for(k=4; k<6; k++)
c[4][5] = a[4][k] * b[k][5];

c

2	11	32	70	130	217	336	492	690	935
0	12	39	86	158	260	397	574	796	1068
0	0	30	83	164	278	430	625	868	1164
0	0	0	56	143	266	430	640	901	1218
0	0	0	0	90	219	392	614	890	1225
0	0	0	0	0	132	311	542	830	1180
0	0	0	0	0	0	182	419	716	1078
0	0	0	0	0	0	0	240	543	914
0	0	0	0	0	0	0	0	306	683
0	0	0	0	0	0	0	0	0	380



Ex1. Matrix Multiplication



```
// KISTI educational Matrix
// Multiplication problem
// Copyright (c) 2012 KISTI
// Supercomputing Center
```

```
PROGRAM ex1
  IMPLICIT NONE
  INTEGER, PARAMETER :: N=9
  INTEGER :: i, j, k, a(0:N,0:N), b(0:N,0:N),
    c(0:N,0:N)
  a = 0
  b = 0
  c = 0
  DO j=0, N
    DO i=0, j
      a(i, j) = i + j + 1
      b(i, j) = i + j + 2
    END DO
  END DO

  DO j=0, N
    DO i=0, j
      DO k=i, j
        c(i, j) = c(i, j) + a(i, k) * b(k, j)
      END DO
    END DO
  END DO
```

a

1	2	3	4	5	6	7	8	9	10
0	3	4	5	6	7	8	9	10	11
0	0	5	6	7	8	9	10	11	12
0	0	0	7	8	9	10	11	12	13
0	0	0	0	9	10	11	12	13	14
0	0	0	0	0	11	12	13	14	15
0	0	0	0	0	0	13	14	15	16
0	0	0	0	0	0	0	15	16	17
0	0	0	0	0	0	0	0	17	18
0	0	0	0	0	0	0	0	0	19

b

2	3	4	5	6	7	8	9	10	11
0	4	5	6	7	8	9	10	11	12
0	0	6	7	8	9	10	11	12	13
0	0	0	8	9	10	11	12	13	14
0	0	0	0	10	11	12	13	14	15
0	0	0	0	0	12	13	14	15	16
0	0	0	0	0	0	14	15	16	17
0	0	0	0	0	0	0	16	17	18
0	0	0	0	0	0	0	0	18	19
0	0	0	0	0	0	0	0	0	20

```
i=4, j=5
for(k=4; k<6; k++)
  c[4][5] = a[4][k] * b[k][5];
```

c

2	11	32	70	130	217	336	492	690	935
0	12	39	86	158	260	397	574	796	1068
0	0	30	83	164	278	430	625	868	1164
0	0	0	56	143	266	430	640	901	1218
0	0	0	0	90	219	392	614	890	1225
0	0	0	0	0	132	311	542	830	1180
0	0	0	0	0	0	182	419	716	1078
0	0	0	0	0	0	0	240	543	914
0	0	0	0	0	0	0	0	306	683
0	0	0	0	0	0	0	0	0	380



Ex1. Matrix Multiplication



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
#include <stdio.h>
#define N 2000
```

```
int main()
{
    int i,j,k;
    int a[N][N], b[N][N], c[N][N];
```

```
    for(i=0; i<N; i++) {
        for(j=0; j<i; j++) {
            a[i][j] = b[i][j] = c[i][j] = 0;
        }
        for(j=i; j<N; j++) {
            a[i][j] = i+j+1;
            b[i][j] = i+j+2;
            c[i][j] = 0;
        }
    }
}
```

```
    for(i=0; i<N; i++)
        for(j=0; j<N; j++)
            for(k=0; k<N; k++)
                c[i][j] += a[i][k] * b[k][j];
}
```

```
$ gcc -o mm0.x mat_mul.c
$ time ./mm0.x
Segmentation fault (core dumped)
$ ulimit -s 512000
$ time ./mm0.x
```



Ex1. Matrix Multiplication



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
PROGRAM ex1
  IMPLICIT NONE
  INTEGER, PARAMETER :: N=1999
  INTEGER :: i, j, k, a(0:N,0:N), b(0:N,0:N), c(0:N,0:N)
  a = 0
  b = 0
  c = 0
  DO j=0, N
    DO i=0, j
      a(i, j) = i + j + 1
      b(i, j) = i + j + 2
    END DO
  END DO

  DO j=0, N
    DO i=0, N
      DO k=0, N
        c(i, j) = c(i, j) + a(i, k) * b(k, j)
      END DO
    END DO
  END DO
```

```
$ gfortran -o mm0.x mat_mul.f90
$ time ./mm0.x
Segmentation fault (core dumped)
$ ulimit -s 512000
$ time ./mm0.x
```



Ex1. Matrix Multiplication



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
#include <stdio.h>
#define N 2000
```

```
int main()
{
    int i,j,k;
    int a[N][N], b[N][N], c[N][N];

    for(i=0; i<N; i++) {
        for(j=0; j<i; j++) {
            a[i][j] = b[i][j] = c[i][j] = 0;
        }
        for(j=i; j<N; j++) {
            a[i][j] = i+j+1;
            b[i][j] = i+j+2;
            c[i][j] = 0;
        }
    }
}
```

```
for(i=0; i<N; i++)
    for(j=i; j<N; j++)
        for(k=i; k<j+1; k++)
            c[i][j] += a[i][k] * b[k][j];
}
```

```
$ gcc -o mm1.x mat_mul.c
$ time ./mm1.x
Segmentation fault (core dumped)
$ ulimit -s 512000
$ time ./mm1.x
```



Ex1. Matrix Multiplication



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
PROGRAM ex1
  IMPLICIT NONE
  INTEGER, PARAMETER :: N=1999
  INTEGER :: i, j, k, a(0:N,0:N), b(0:N,0:N), c(0:N,0:N)
  a = 0
  b = 0
  c = 0
  DO j=0, N
    DO i=0, j
      a(i, j) = i + j + 1
      b(i, j) = i + j + 2
    END DO
  END DO

  DO j=0, N
    DO i=0, j
      DO k=i, j
        c(i, j) = c(i, j) + a(i, k) * b(k, j)
      END DO
    END DO
  END DO
```

```
$ gcc -o mm1.x mat_mul.c
$ time ./mm1.x
Segmentation fault (core dumped)
$ ulimit -s 512000
$ time ./mm1.x
```



Ex1. Matrix Multiplication (Apply OpenMP)



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
#include <stdio.h>
#define N 2000
int main()
{
    int i,j,k;
    int a[N][N], b[N][N], c[N][N];

    #pragma omp parallel for ???
    for(i=0; i<N; i++) {
        #pragma omp sections ???
        for(j=0; j<i; j++) {
            a[i][j] = b[i][j] = c[i][j] = 0;
        }
        for(j=i; j<N; j++) {
            a[i][j] = i+j+1;
            b[i][j] = i+j+2;
            c[i][j] = 0;
        }
    }
}
```

```
#pragma omp parallel for ???
for(i=0; i<N; i++)
    for(j=i; j<N; j++)
        for(k=i; k<j+1; k++)
            c[i][j] += a[i][k] * b[k][j];
}
```

```
$ export OMP_NUM_THREADS=4
$ gcc -o mm2.x mat_mul.c
$ time ./mm2.x
Segmentation fault (core dumped)
$ ulimit -s 512000
$ time ./mm2.x
```



Ex1. Matrix Multiplication (Apply OpenMP)



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
PROGRAM ex1
  IMPLICIT NONE
  INTEGER, PARAMETER :: N=1999
  INTEGER :: i, j, k, a(0:N,0:N), b(0:N,0:N), c(0:N,0:N)
  a = 0
  b = 0
  c = 0
```

!\$omp parallel do???

```
DO j=0, N
  DO i=0, j
    a(i, j) = i + j + 1
    b(i, j) = i + j + 2
  END DO
END DO
```

!\$omp parallel do???

```
DO j=0, N
  DO i=0, j
    DO k=i, j
      c(i, j) = c(i, j) + a(i, k) * b(k, j)
    END DO
  END DO
END DO
```

```
$ export OMP_NUM_THREADS=4
$ gcc -o mm2.x mat_mul.c
$ time ./mm2.x
Segmentation fault (core dumped)
$ ulimit -s 512000
$ time ./mm2.x
```



Ex1. Matrix Multiplication (Apply OpenMP)



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
#include <stdio.h>
#define N 2000
int main()
{
    int i,j,k;
    int a[N][N], b[N][N], c[N][N];

    #pragma omp parallel for private(j)
    for(i=0; i<N; i++) {
        for(j=0; j<i; j++) {
            a[i][j] = b[i][j] = c[i][j] = 0;
        }
        for(j=i; j<N; j++) {
            a[i][j] = i+j+1;
            b[i][j] = i+j+2;
            c[i][j] = 0;
        }
    }
}
```

```
#pragma omp parallel for private(j,k)
for(i=0; i<N; i++)
    for(j=i; j<N; j++)
        for(k=i; k<j+1; k++)
            c[i][j] += a[i][k] * b[k][j];
}
```

```
$ export OMP_NUM_THREADS=4
$ gcc -o mm3.x mat_mul.c
$ time ./mm3.x
Segmentation fault (core dumped)
$ ulimit -s 512000
$ time ./mm3.x
```



Ex1. Matrix Multiplication (Apply OpenMP)



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
PROGRAM ex1
  IMPLICIT NONE
  INTEGER, PARAMETER :: N=1999
  INTEGER :: i, j, k, a(0:N,0:N), b(0:N,0:N), c(0:N,0:N)
  a = 0
  b = 0
  c = 0
```

```
!$omp parallel do private(i)
```

```
  DO j=0, N
    DO i=0, j
      a(i, j) = i + j + 1
      b(i, j) = i + j + 2
    END DO
  END DO
```

```
!$omp parallel do private(i,k)
```

```
  DO j=0, N
    DO i=0, j
      DO k=i, j
        c(i, j) = c(i, j) + a(i, k) * b(k, j)
      END DO
    END DO
  END DO
```

```
$ export OMP_NUM_THREADS=4
$ gcc -o mm3.x mat_mul.c
$ time ./mm3.x
Segmentation fault (core dumped)
$ ulimit -s 512000
$ time ./mm3.x
```



Ex1. Matrix Multiplication (Apply OpenMP)



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
#include <stdio.h>
#define N 2000
int main()
{
    int i,j,k;
    int a[N][N], b[N][N], c[N][N];

    #pragma omp parallel for private(j)
    for(i=0; i<N; i++) {
        for(j=0; j<i; j++) {
            a[i][j] = b[i][j] = c[i][j] = 0;
        }
        for(j=i; j<N; j++) {
            a[i][j] = i+j+1;
            b[i][j] = i+j+2;
            c[i][j] = 0;
        }
    }
}
```

```
#pragma omp parallel for private(j,k) schedule(dynamic,5)
for(i=0; i<N; i++)
    for(j=i; j<N; j++)
        for(k=i; k<j+1; k++)
            c[i][j] += a[i][k] * b[k][j];
}
```

```
$ export OMP_NUM_THREADS=4
$ gcc -o mm4.x mat_mul.c
$ time ./mm4.x
Segmentation fault (core dumped)
$ ulimit -s 512000
$ time ./mm4.x
```



Ex1. Matrix Multiplication (Apply OpenMP)



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
PROGRAM ex1
  IMPLICIT NONE
  INTEGER, PARAMETER :: N=1999
  INTEGER :: i, j, k, a(0:N,0:N), b(0:N,0:N), c(0:N,0:N)
  a = 0
  b = 0
  c = 0
```

```
!$omp parallel do private(i)
```

```
  DO j=0, N
    DO i=0, j
      a(i, j) = i + j + 1
      b(i, j) = i + j + 2
    END DO
  END DO
```

```
!$omp parallel do private(i,k) schedule(dynamic,5)
```

```
  DO j=0, N
    DO i=0, j
      DO k=i, j
        c(i, j) = c(i, j) + a(i, k) * b(k, j)
      END DO
    END DO
  END DO
```

```
$ export OMP_NUM_THREADS=4
$ gcc -o mm4.x mat_mul.c
$ time ./mm4.x
Segmentation fault (core dumped)
$ ulimit -s 512000
$ time ./mm4.x
```



Ex2. LU Decomposition - C (Serial)



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
#include <stdio.h>
```

```
#define N 5
```

```
void LU_decomp(double A[N][N])
```

```
{
    int i, j, k;
    double aij;
    for(j = 0; j < N-1; j++) {
        aij = A[j][j];
        if( aij != 0.0 ) {
            for(i=j+1; i<N; i++) {
                A[i][j] /= aij;
                for(k=j+1; k<N; k++)
                    A[i][k] -= (A[i][j] * A[j][k]);
            }
        }
    }
}
```

```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
int main()
```

```
{
    double A[N][N];
    int i;
    for(i=0; i<N; i++)
        A[i][j] = rand() % 100 + 5.0;

    for(i=0; i<N; i++) {
        for(j=0; j<N; j++)
            printf("%lf ", A[i][j]);
        printf("\n");
    }
    printf("\n");
    LU_decomp(A);
    for(i=0; i<N; i++) {
        for(j=0; j<N; j++)
            printf("%lf ", A[i][j]);
        printf("\n");
    }
}
```



Ex2. LU Decomposition - Fortran(Serial)



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
PROGRAM LU
IMPLICIT NONE
```

```
INTEGER,PARAMETER :: N=5
INTEGER :: i, j
DOUBLE PRECISION :: A(0:N-1, 0:N-1)
```

```
DO i=0, N-1
  CALL random_number( A(i, j) )
  A(i, j) = nint(A(i, j) * 100) + 5.0
END DO
```

```
CALL LU_decomp(A, N);
```

```
DO i=0, N-1
  WRITE(*, 100) (c(i, j), j=0, N-1)
END DO
```

```
100 FORMAT(10(F8.3))
END
```

```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
SUBROUTINE LU_decomp(A, N)
```

```
  INTEGER :: i, j, k, N;
  DOUBLE PRECISION :: aji, A(0:N-1, 0:N-1)
```

```
  DO j=0, N-2
    aji = A(j, j);
    if( aji /= 0.0 ) THEN
      DO i=j+1, N-1
        A(i, j) = A(i, j) / aji;
        DO k=j+1, N-1
          A(i, k) = A(i, k) - ( A(i, j) * A(j, k) );
        END DO
      END DO
    END IF
  END DO
END SUBROUTINE
```



Ex2. LU Decomposition - C(Parallel) Step 1



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
#include <stdio.h>
```

```
#define N 5
```

```
void LU_decomp(double A[N][N])
```

```
{
```

```
    int i, j, k;
```

```
    double aij;
```

```
    #pragma omp parallel for private(i,j,k,aij)
```

```
    for(j = 0; j < N-1; j++) {
```

```
        aij = A[j][j];
```

```
        if( aij != 0.0 ) {
```

```
            for(i=j+1; i<N; i++) {
```

```
                A[i][j] /= aij;
```

```
                for(k=j+1; k<N; k++)
```

```
                    A[i][k] -= (A[i][j] * A[j][k]);
```

```
            }
```

```
    }
```

```
}
```

```
    j=0
```

```
    i=1; i<N
```

```
    k=1; k<N
```

```
    A[i][k] -= (A[i][0]*A[0][k])
```

```
    j=2
```

```
    i=3; i<N
```

```
    k=3; k<N
```

```
    A[i][k] -= (A[i][2]*A[2][k])
```

No problem ???

```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
int main()
```

```
{
```

```
    double A[N][N];
```

```
    int i;
```

```
    for(i=0; i<N; i++)
```

```
        A[i][j] = rand() % 100 + 5.0;
```

```
    for(i=0; i<N; i++) {
```

```
        for(j=0; j<N; j++)
```

```
            printf("%lf ", A[i][j]);
```

```
        printf("\n");
```

```
    }
```

```
    printf("\n");
```

```
    LU_decomp(A);
```

```
    for(i=0; i<N; i++) {
```

```
        for(j=0; j<N; j++)
```

```
            printf("%lf ", A[i][j]);
```

```
        printf("\n");
```

```
    }
```

```
}
```



Ex2. LU Decomposition - Fortran(Parallel) Step1



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
PROGRAM LU
IMPLICIT NONE
```

```
INTEGER,PARAMETER :: N=5
INTEGER :: i, j
DOUBLE PRECISION :: A(0:N-1, 0:N-1)
```

```
DO i=0, N-1
  CALL random_number( A(i, j) )
  A(i, j) = nint(A(i, j) * 100) + 5.0
END DO
```

```
CALL LU_decomp(A, N);
```

```
DO i=0, N-1
  WRITE(*, 100) (c(i, j), j=0, N-1)
END DO
```

```
100 FORMAT(10(F8.3))
```

```
END
```

```
j=0
do i=1, N-1
  do k=1, N-1
    A(i,k) = A(i,k) - ( A(i,0)*A(0,k) )
```

```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
SUBROUTINE LU_decomp(A, N)
  INTEGER :: i, j, k, N;
  DOUBLE PRECISION :: ajj, A(0:N-1, 0:N-1)
```

```
!$omp parallel for private(i,j,k,ajj)
```

```
DO j=0, N-2
  ajj = A(j, j);
  if( ajj /= 0.0 ) THEN
```

```
    DO i=j+1, N-1
```

```
      A(i, j) = A(i, j) / ajj;
```

```
      DO k=j+1, N-1
```

```
        A(i, k) = A(i, k) - ( A(i, j) * A(j, k) );
```

```
      END DO
```

```
    END DO
```

```
  END IF
```

```
END DO
```

```
!$omp end parallel for
```

```
END SUBROUTINE
```

```
j=2
do i=3, N-1
  do k=3, N-1
    A(i,k) = A(i,k) - ( A(i,2)*A(2,k) )
```

No problem ???



Ex2. LU Decomposition - C(Parallel) Step 2



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
#include <stdio.h>
```

```
#define N 5
```

```
void LU_decomp(double A[N][N])
```

```
{
```

```
    int i, j, k;
```

```
    double aij;
```

```
    #pragma omp parallel for private(i,j,k,aij)
```

```
    for(j = 0; j < N-1; j++) {
```

```
        aij = A[j][j];
```

```
        if( aij != 0.0 ) {
```

```
            for(i=j+1; i<N; i++) {
```

```
                A[i][j] /= aij;
```

```
                for(k=j+1; k<N; k++)
```

```
                    #pragma omp atomic
```

```
                    A[i][k] -= (A[i][j] * A[j][k]);
```

```
            }
```

```
        }
```

```
    }
```

```
}
```

No problem ???

```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
int main()
```

```
{
```

```
    double A[N][N];
```

```
    int i;
```

```
    for(i=0; i<N; i++)
```

```
        A[i][j] = rand() % 100 + 5.0;
```

```
    for(i=0; i<N; i++) {
```

```
        for(j=0; j<N; j++)
```

```
            printf("%lf ", A[i][j]);
```

```
            printf("\n");
```

```
    }
```

```
    printf("\n");
```

```
    LU_decomp(A);
```

```
    for(i=0; i<N; i++) {
```

```
        for(j=0; j<N; j++)
```

```
            printf("%lf ", A[i][j]);
```

```
            printf("\n");
```

```
    }
```

```
}
```



Ex2. LU Decomposition - Fortran(Parallel) Step2



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
PROGRAM LU
IMPLICIT NONE
```

```
INTEGER,PARAMETER :: N=5
INTEGER :: i, j
DOUBLE PRECISION :: A(0:N-1, 0:N-1)
```

```
DO i=0, N-1
  CALL random_number( A(i, j) )
  A(i, j) = nint(A(i, j) * 100) + 5.0
END DO
```

```
CALL LU_decomp(A, N);
```

```
DO i=0, N-1
  WRITE(*, 100) (c(i, j), j=0, N-1)
END DO
```

```
100 FORMAT(10(F8.3))
END
```

```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
SUBROUTINE LU_decomp(A, N)
```

```
  INTEGER :: i, j, k, N;
  DOUBLE PRECISION :: aij, A(0:N-1, 0:N-1)
```

```
!$omp parallel for private(i,j,k,aij)
```

```
  DO j=0, N-2
    aij = A(j, j);
    if( aij /= 0.0 ) THEN
```

```
      DO i=j+1, N-1
```

```
        A(i, j) = A(i, j) / aij;
```

```
        DO k=j+1, N-1
```

```
          !$omp atomic
```

```
            A(i, k) = A(i, k) - ( A(i, j) * A(j, k) );
```

```
          END DO
```

```
        END DO
```

```
      END IF
```

```
    END DO
```

```
!$omp end parallel for
```

```
END SUBROUTINE
```

No problem ???



Ex2. LU Decomposition - C(Parallel) Solution



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
#include <stdio.h>
#define N 5

void LU_decomp(double A[N][N])
{
    int i, j, k;
    double aij;
    for(j = 0; j < N-1; j++) {
        aij = A[j][j];
        if( aij != 0.0 ) {
            #pragma omp parallel for private(i,k)
            for(i=j+1; i<N; i++) {
                A[i][j] /= aij;
                for(k=j+1; k<N; k++)
                    A[i][k] -= (A[i][j] * A[j][k]);
            }
        }
    }
}
```

```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
int main()
{
    double A[N][N];
    int i;
    for(i=0; i<N; i++)
        A[i][j] = rand() % 100 + 5.0;

    for(i=0; i<N; i++) {
        for(j=0; j<N; j++)
            printf("%lf ", A[i][j]);
        printf("\n");
    }
    printf("\n");
    LU_decomp(A);
    for(i=0; i<N; i++) {
        for(j=0; j<N; j++)
            printf("%lf ", A[i][j]);
        printf("\n");
    }
}
```



Ex2. LU Decomposition - Fortran(Parallel) Solution



```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
PROGRAM LU
IMPLICIT NONE
```

```
INTEGER,PARAMETER :: N=5
INTEGER :: i, j
DOUBLE PRECISION :: A(0:N-1, 0:N-1)
```

```
DO i=0, N-1
  CALL random_number( A(i, j) )
  A(i, j) = nint(A(i, j) * 100) + 5.0
END DO
```

```
CALL LU_decomp(A, N);
```

```
DO i=0, N-1
  WRITE(*, 100) (c(i, j), j=0, N-1)
END DO
```

```
100 FORMAT(10(F8.3))
END
```

```
// KISTI educational Matrix Multiplication problem
// Copyright (c) 2012 KISTI Supercomputing Center
```

```
SUBROUTINE LU_decomp(A, N)
```

```
  INTEGER :: i, j, k, N;
  DOUBLE PRECISION :: aij, A(0:N-1, 0:N-1)
  DO j=0, N-2
    aij = A(j, j);
    if( aij /= 0.0 ) THEN
```

```
      !$omp parallel for private(i,k)
```

```
      DO i=j+1, N-1
        A(i, j) = A(i, j) / aij;
        DO k=j+1, N-1
          A(i, k) = A(i, k) - ( A(i, j) * A(j, k) );
        END DO
      END DO
```

```
      !$omp end parallel for
```

```
    END IF
  END DO
END SUBROUTINE
```



Ex3. Fibonacci



Fortran	C
<pre> PROGRAM fibonacci IMPLICIT NONE INTEGER :: result result = fibon(MAX) PRINT *, "Fibonacci (", MAX, ") =", result contains recursive INTEGER function fibon(n) RESULT(fib) IMPLICIT NONE INTEGER :: n, x, y if(n<2) THEN fib=n else x=fibon(n-1); y=fibon(n-2); fib = x + y END function END </pre>	<pre> #include <stdio.h> int fibon(int n) // f(n) = f(n-1) + f(n-2) { int x, y; if(n<2) return n; x=fibon(n-1); y=fibon(n-2); return (x+y); } int main() { int result = fibon(MAX); printf("Fibonacci (%d) = %d\n", MAX, result); return 0; } </pre>
<pre> \$ gfortran -DMAX=40 -o fibon.x fibonacci.f90 \$./fibon.x </pre>	<pre> \$ gcc -DMAX=40 -o fibon.x fibonacci.c \$./fibon.x </pre>



Ex3. Fibonacci (Solution with Task)



Fortran	C
<pre> PROGRAM fibonacci USE OMP_LIB or include "omp_lib.h" INTEGER :: result !\$omp parallel !\$OMP SINGLE result = fibon(MAX) !\$omp end SINGLE !\$omp end parallel PRINT *, "Fibonacci (" , MAX, ") = ", result END recursive INTEGER function fibon(n) RESULT(fib) INTEGER :: n, x, y if(n<2) THEN fib = n else !\$OMP TASK shared(x) x=fibon(n-1) !\$omp end TASK !\$OMP TASK shared(y) y=fibon(n-2) !\$omp end TASK !\$OMP TASKWAIT fib = x + y END IF END function </pre>	<pre> #include <stdio.h> #include <omp.h> int fibon(int n) // f(n) = f(n-1) + f(n-2) { int x, y; if(n<2) return n; #pragma omp task shared(x) { x=fibon(n-1); } #pragma omp task shared(y) { y=fibon(n-2); } #pragma omp taskwait return (x+y); } int main() { int result; #pragma omp parallel { #pragma omp single result = fibon(MAX); } printf("Fibonacci (%d) = %d\n", MAX, result); return 0; } </pre>
<pre> \$ gfortran -DMAX=40 -o fibon2.x fibonacci2.f90 \$./fibon2.x </pre>	<pre> \$ gcc -DMAX=40 -o fibon2.x fibonacci2.c \$./fibon2.x </pre>



Ex3. Fibonacci (Optimized Solution with Task)



Fortran	C
<pre>PROGRAM fibonacci USE OMP_LIB or include "omp_lib.h" INTEGER :: result, fibon !\$omp parallel !\$OMP SINGLE result = fibon(MAX) !\$omp end SINGLE !\$omp end parallel PRINT *, "Fibonacci (" , MAX, ") =" , result contains recursive INTEGER function fibon(n) RESULT(fib) INTEGER n, x , y if(n<2) THEN fib = n else if(n>30) THEN fib = fibon(n-1) + fibon(n-2) else !\$OMP TASK shared(x) x=fibon(n-1) !\$omp end TASK !\$OMP TASK shared(y) y=fibon(n-2) !\$omp end TASK !\$OMP TASKWAIT fib = x + y END function END</pre>	<pre>#include <stdio.h> #include <omp.h> int fibon(int n) // f(n) = f(n-1) + f(n-2) { int x, y; if(n<2) return n; if(n<30) return fibon(n-1)+fibon(n-2); #pragma omp task shared(x) { x=fibon(n-1); } #pragma omp task shared(y) { y=fibon(n-2); } #pragma omp taskwait return (x+y); } int main() { int result; #pragma omp parallel { #pragma omp single result = fibon(MAX); } printf("Fibonacci (%d) = %d\n", MAX, result); return 0; }</pre>

Q&A

A large, 3D red question mark is positioned to the right of the "Q&A" text. The entire graphic is set against a light gray, tilted rectangular background.

Thank
you

A yellow 3D figure is positioned to the right of the text "Thank you". The figure is pointing its right index finger towards the word "you".